

Measurement of γ using $B^\pm \rightarrow D_{\pi^- \pi^+ \pi^0} K^\pm$
with Dalitz Plot Analysis of $D^0 \rightarrow \pi^- \pi^+ \pi^0$

Kalanand Mishra

University of Cincinnati

BaBar collaboration



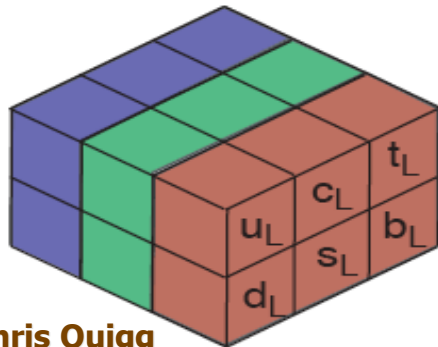
Weak interaction of quarks in SM

Elementary Particles						
Leptons	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino	γ photon	Force Carriers	g gluon
	e electron	μ muon	τ tau	Z Z boson		W W boson
	III Three Families of Matter					
Quarks	u up	c charm	t top			
	d down	s strange	b bottom			
	II					

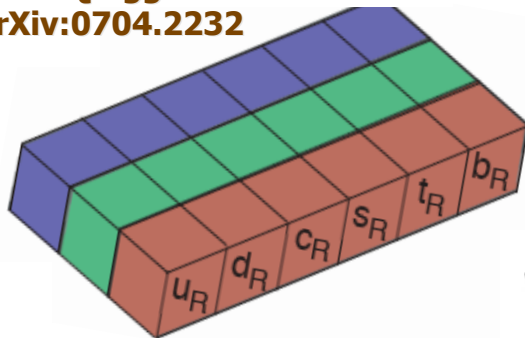
Left handed quarks in doublets $q_L^i = \begin{pmatrix} u_L^i \\ d_L^i \end{pmatrix}$

Right handed quarks in singlets \Rightarrow do not couple to W

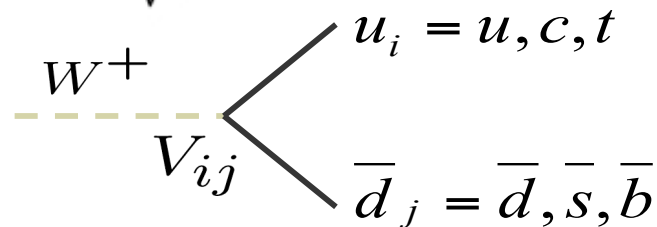
- The electroweak coupling strength of W to left-handed quarks is described by Cabibbo-Kobayashi-Maskawa matrix



Chris Quigg
arXiv:0704.2232



$$-\mathcal{L}_{W^\pm} = \frac{g}{\sqrt{2}} \bar{u}_{Li} \gamma^\mu (V_{CKM})_{ij} d_{Lj} W_\mu^\pm + \text{h.c.}$$

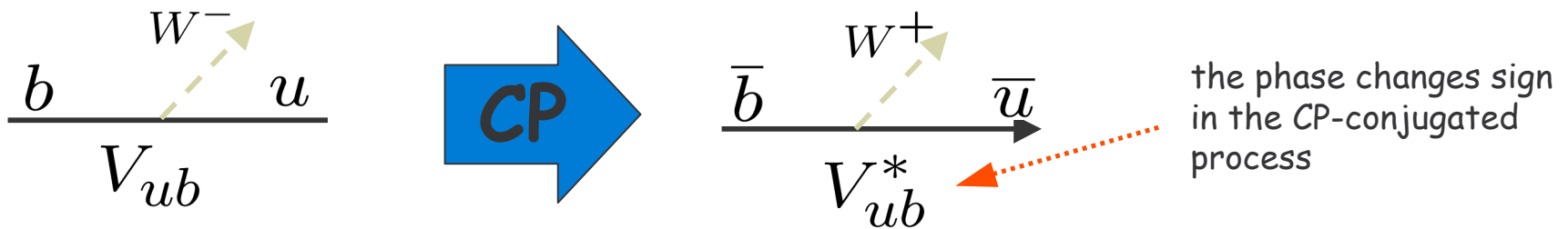


- 3x3 unitary matrix \Rightarrow 4 parameters

$$V = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} \blacksquare & \blacksquare & \cdot \\ \blacksquare & \blacksquare & \cdot \\ \cdot & \blacksquare & \blacksquare \end{pmatrix} \quad \text{relative magnitude of the elements}$$

The CKM Matrix

- An irremovable complex phase in V_{CKM} is the origin of CP violation in the SM



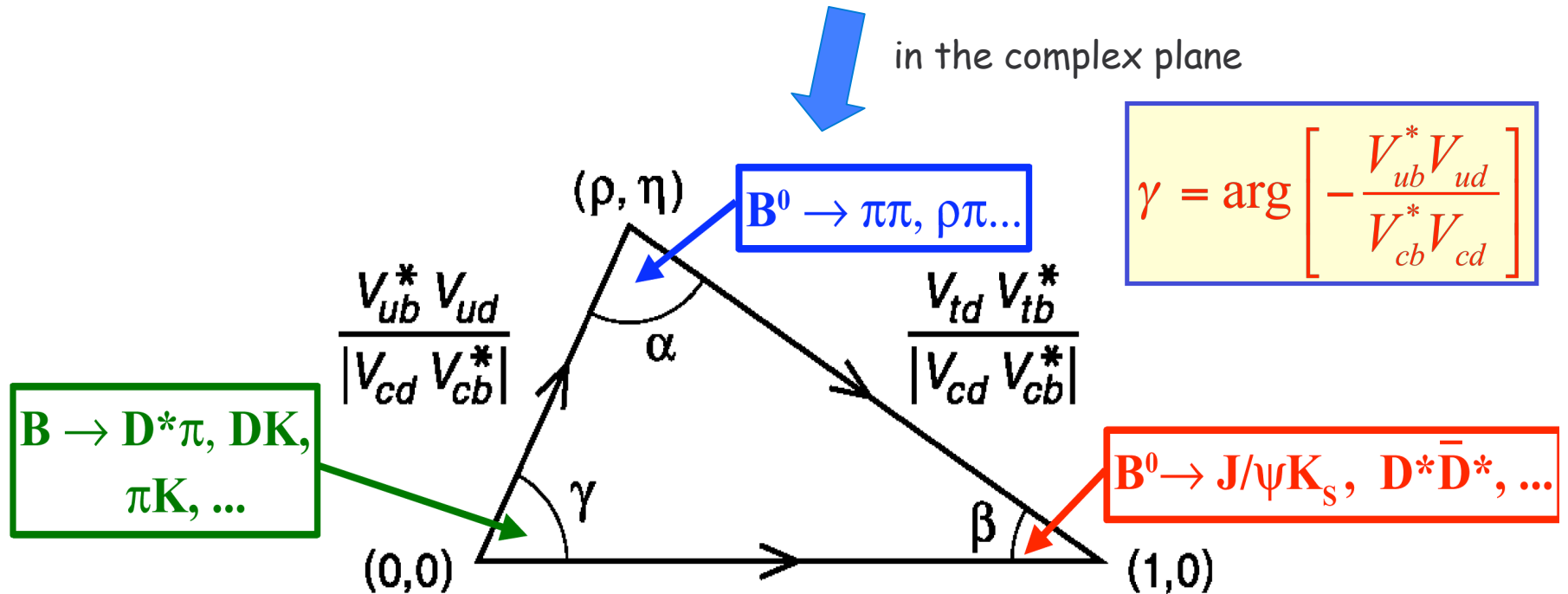
- In the Wolfenstein parameterization:

$$V = \begin{pmatrix} 1 - \frac{\lambda^2}{2} & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{\lambda^2}{2} & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + \mathcal{O}(\lambda^4)$$

The Unitarity Triangle

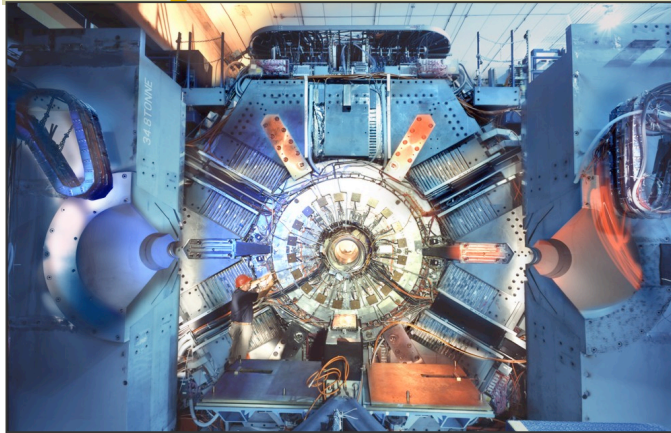
- V is unitary: $VV^+ = 1 \Rightarrow V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$

in the complex plane



- Expect γ to be $\sim (60 \pm 10)^\circ$, if the Standard Model is consistent.
- But need to *measure* it directly, need redundant measurements
- Several ways to measure γ , no single one of them is “silver bullet” !

BaBar: B and charm Factory



Electromagnetic Calorimeter
6580 CsI crystals
 e^+ ID, π^0 and γ reco

Instrumented Flux Return
12-18 layers of RPC/LST
 μ ID

e^+ [3.1 GeV]

Cherenkov Detector
144 quartz bars
K, π , p separation

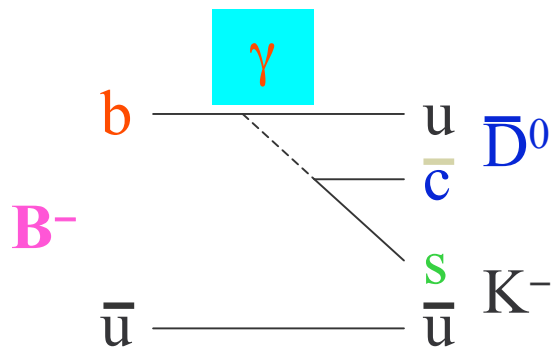
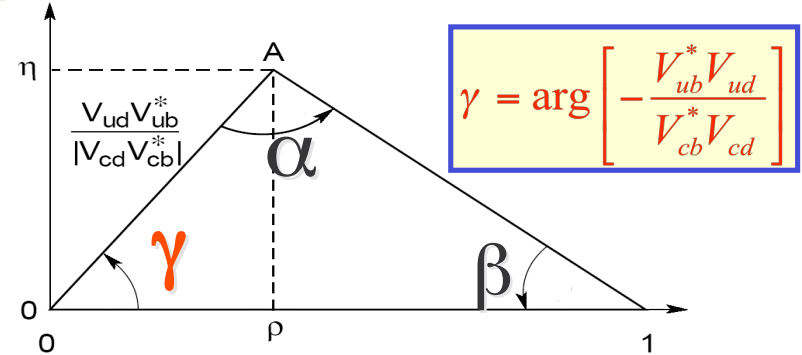
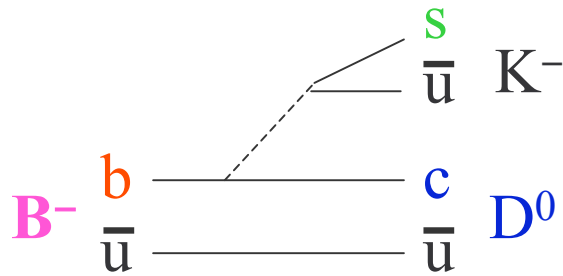
Drift Chamber
40 layers
tracking + dE/dx

e^- [9 GeV]

1.5T Magnet

Silicon Vertex Tracker
5 layers (double-sided Si sensors)
vertexing + tracking (+ dE/dx)

Extraction of γ with $B \rightarrow D^0 K$



Common final state f

Secret to Success:

interference between color-allowed $D^0 K$ and color-suppressed $\bar{D}^0 K$ amplitudes.

Decay time-independent!

Color suppression

$$\text{Magnitude ratio} \equiv r_B \approx \left| \frac{V_{ub}}{V_{cb}} \cdot \frac{V_{cs}}{V_{us}} \right| \cdot \frac{1}{N_{\text{colors}}} \approx \frac{\rho - i\eta}{N_{\text{colors}}} \approx \frac{0.4}{3} \approx 0.1$$

The bigger the better!

Larger $r_B \Rightarrow$ larger interference term \Rightarrow better constraints on γ .

A Simple Interference Algebra

$$\text{Amplitude 1} = A e^{i\gamma}$$

$$\text{Amplitude 2} = B e^{i\delta}$$

$$\text{Total amplitude} = A e^{i\gamma} + B e^{i\delta}$$

$$\text{Decay Rate} = A^2 + B^2 + 2AB \cos(\delta - \gamma)$$

Decay Rate of CP-conjugate decay

$$= A^2 + B^2 + 2AB \cos(\delta + \gamma)$$

If 2 parameters are known (A/B and δ), use the 2 equations to solve for B and γ .

$B \rightarrow DK$, through a slightly more complicated analysis, allows you to measure γ when δ is not known.

Evolution of Methods on γ

- **Gronau, Landon, and Wyler (GLW) Phys. Lett. B 265, 172 (1991)**
 - This was the original $B \rightarrow DK$ paper. Reconstruct D in a CP eigenstate.
 - Additional measurements are needed to determine them all: r_B, δ, γ .

Main Drawback:

$BF(B \rightarrow DK) \sim 10^{-4}, BF(D \rightarrow f_{CP}) \sim 10^{-2}$
Small... \Rightarrow strongly statistics limited

- **Atwood, Dunietz, and Soni (ADS), Phys. Rev. Lett. 78, 3257 (1997)**
 - Noted the sizable interference between the DCS and CF decays of D , and proposed to use them, to realize the interference.
 - Method can't be used standalone either, since there is only one 2-body DCS mode, $D^0 \rightarrow K^+ \pi^-$, while at least 2 modes are needed. Need additional input of strong phase difference in D decays.

No significant signal with current data

- **Giri, Grossman, Soffer, Zupan (GGSZ) Phys. Rev. D68, 054018 (2003)**
 - Outlines the method for using multi-body D decays with model-dependent and -independent analysis

Will elaborate on this later

- **BaBar, hep-ex/0507101 and Belle, hep-ex/0504013 (2005)**
 - The experimental measurements of γ using $B \rightarrow DK, D \rightarrow K_S \pi^+ \pi^-$

- **Bondar, A. Poluektov, ph/0510246 (2005)**
 - MC study of the model-independent (binned Dalitz plot) measurement of γ

Discrete Ambiguities

- The observables are $\cos(\delta + \gamma)$ and $\cos(\delta - \gamma)$, which are invariant under
 - ✓ $\mathbf{S}_{\text{ex}} : \delta \leftrightarrow \gamma$
 - ✓ $\mathbf{S}_{\pm} : \delta \rightarrow -\delta, \quad \gamma \rightarrow -\gamma$
 - ✓ $\mathbf{S}_{\pi} : \delta \rightarrow \delta + \pi, \quad \gamma \rightarrow \gamma + \pi$
- If δ_f and $\delta_{f'}$ are different enough, \mathbf{S}_{ex} is resolved, since you can't simultaneously satisfy both $\delta_f \leftrightarrow \gamma$ and $\delta_{f'} \leftrightarrow \gamma$

While measuring γ , one encounters two devils: statistics and ambiguity, and they often feed each other.

2-body vs Multi-body D^0 Final States

Advantages of multi-body final states:

- Effectively, provide many final states, due to the variation of r_f and δ_f . This helps to resolve ambiguities down to an irreducible 2-fold ambiguity :)
- Add statistics – access to modes for which the 2-body final-state technique for measuring γ is not applicable :)

Disadvantages:

- More complicated analysis :(
- New systematic errors (how well do we understand the D final-state phase-space distribution?) unless using model-independent analysis approach :(

Overall:

- A-priori, both kinds of states are approximately equally useful in measuring γ . Measurement is statistically limited, need all the modes we can get. In practice, some modes will turn out to be more useful than others.

Analysis Steps for $B^\pm \rightarrow D_{\pi^-\pi^+\pi^0} K^\pm$

Step 1: Obtain $D^0 \rightarrow \pi^+\pi^-\pi^0$ Dalitz Plot parameterization using $D^{*+} \rightarrow D^0\pi^+$ (and c.c) sample

Step 2: Fit $B^- \rightarrow D_{\pi\pi\pi^0} K^-$ (and c.c) sample to obtain signal yield and branching-ratio asymmetry

Step 3: Fit for CP parameters using results of Steps 1 and 2 on $B^- \rightarrow D_{\pi\pi\pi^0} K^-$ sample

Step 1

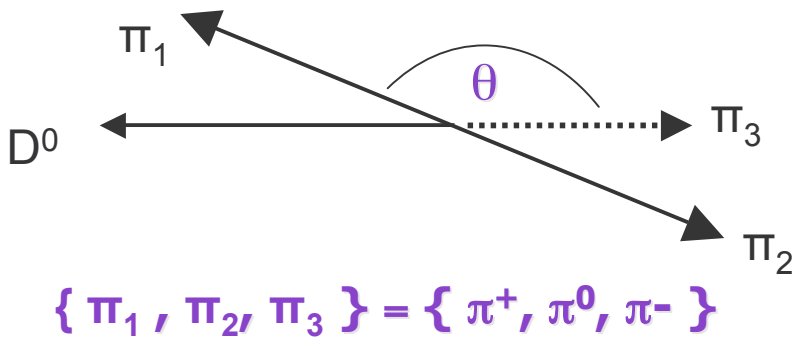
3-Particle Phase Space

■ **2 Observables**

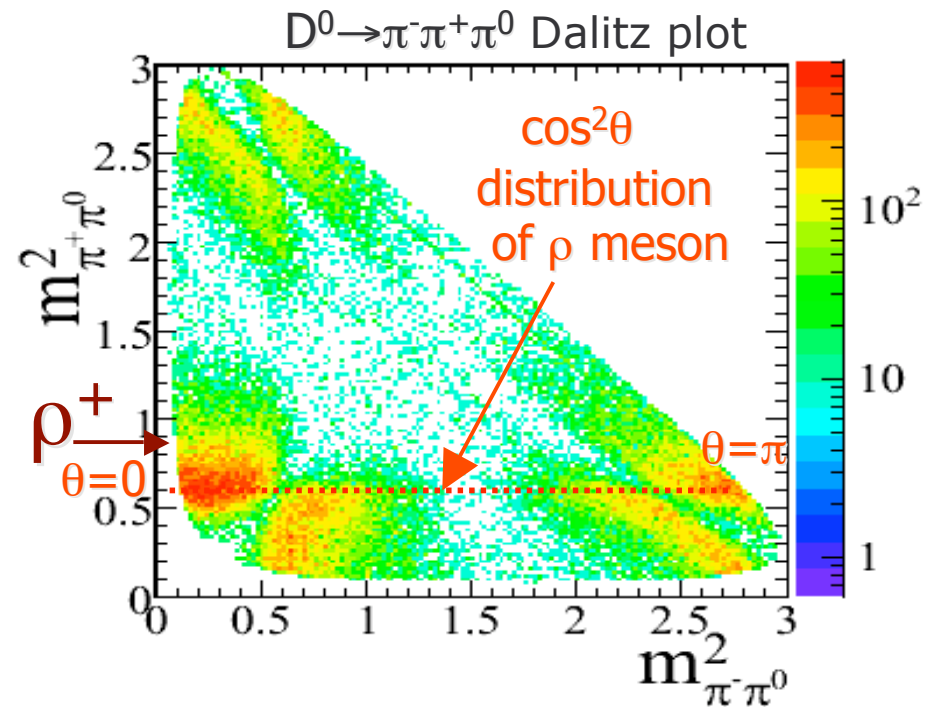
From four vectors	12
Conservation laws	-4
Final state particle masses	-3
Free rotation in decay plane	-3
Σ	2

■ **Usual choice**

Invariant mass squared m_{12}^2
 Invariant mass squared m_{13}^2



- Dalitz plot provides info on angular distr.
- Also about dynamical amplitudes involved.
- Flat if no dynamics involved.

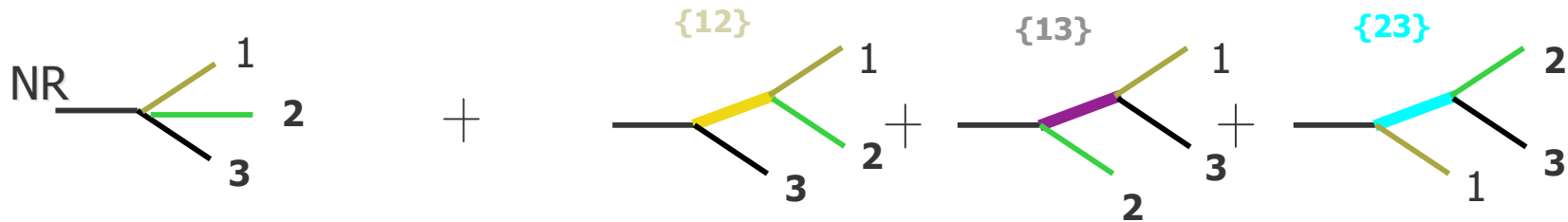


- Dalitz applied this method first to K_L -decays
 - To resolve τ/θ puzzle with only few events
 - goal was to determine spin and parity
- And he never called them Dalitz plots !

Step 1

Isobar Model Formalism

three-body decay $D \rightarrow ABC$ decaying through an $r=[AB]$ resonance



D decay three-body amplitude $\mathcal{A}_D(s_{12}, s_{13}) = a_0 e^{i\delta_0} + \sum_r a_r e^{i\delta_r} \mathcal{A}_r(s_{12}, s_{13})$

$a_0, \delta_0, a_r, \delta_r$: Free parameters of fit

NR term (direct 3 body decay)

$$\mathcal{A}_r(s_{12}, s_{13}) = F_D^J F_r^J \times M_r^J \times BW_r^J$$

Relativistic Breit-Wigner

$$BW_r^J(s) = \begin{cases} \frac{1}{M_r^2 - s - iM_r\Gamma_r(\sqrt{s})} & f_0(980) \\ \frac{1}{M_r^2 - s - i(\rho_1 g_1^2 + \rho_2 g_2^2)} & a_0(980) \end{cases}$$

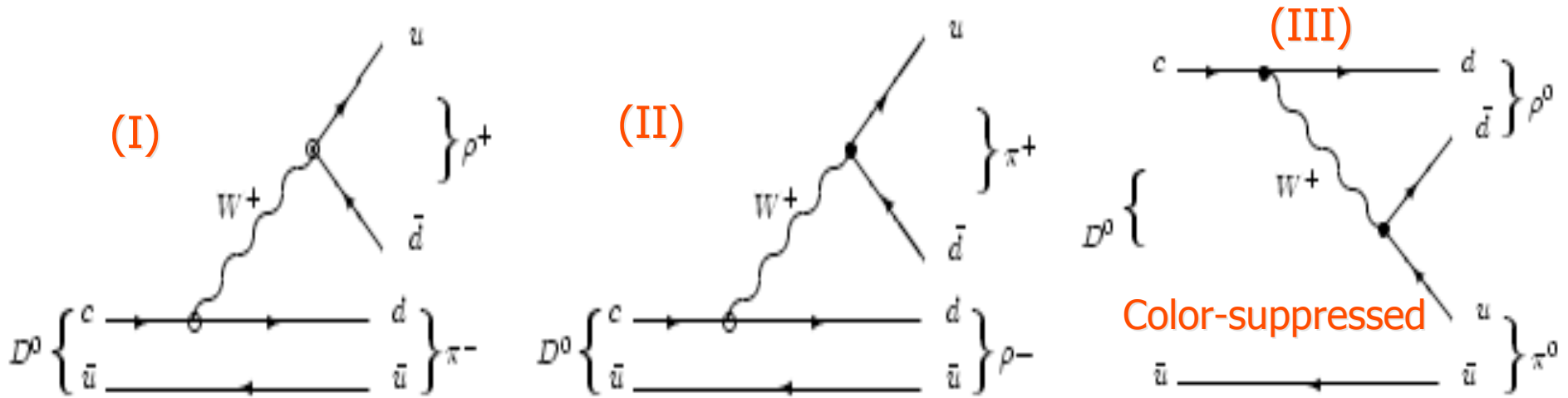
Angular distribution

D and r Blatt-Weisskopf form factors

Step 1

$D^0 \rightarrow \pi^- \pi^+ \pi^0$ Dalitz Plot Amplitudes

Interference between three types of singly Cabibbo-suppressed amplitudes



$$\mathcal{A}[D^0 \rightarrow \pi^- \pi^+ \pi^0] \equiv f_{D^0}(m_{\pi^+ \pi^0}^2, m_{\pi^- \pi^0}^2)$$

$$\bar{\mathcal{A}}[\bar{D}^0 \rightarrow \pi^+ \pi^- \pi^0] \equiv f_{D^0}(m_{\pi^- \pi^0}^2, m_{\pi^+ \pi^0}^2)$$

$$m_{\pi^+ \pi^0}^2 + m_{\pi^- \pi^0}^2 + m_{\pi^+ \pi^-}^2 = m_{\pi^+}^2 + m_{\pi^-}^2 + m_{\pi^0}^2 + m_{D^0}^2$$

PDF for signal events = $|f|^2$

Assumes no D -mixing, no CP violation in D decays!

Step 1

$D^0 \rightarrow \pi^- \pi^+ \pi^0$ Event Reconstruction

$D^0 \rightarrow \pi^- \pi^+ \pi^0$ Reconstruction

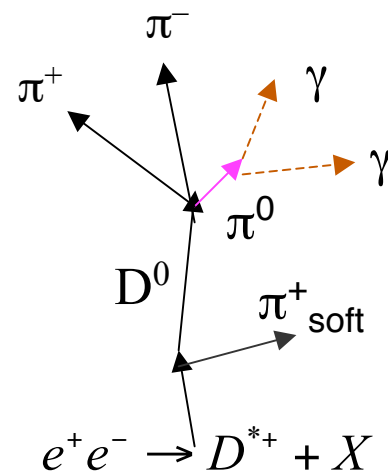
- π^- and π^+ tracks are fit to a vertex
- Mass of π^0 candidate is constrained to m_{π^0} at $\pi^- \pi^+$ vertex
- $P_{\text{CM}}(D^0) > 2.77 \text{ GeV}/c$

D^* Reconstruction

- D^{*+} candidate is made by fitting the D^0 and π_s^+ to a vertex constrained in x and y to the measured beam-spot.
- $|m_{D^{*+}} - m_{D^0} - 145.5| < 0.6 \text{ MeV}/c^2$
- Vertex χ^2 probability > 0.01
- Choose the best candidate per event with the smallest χ^2 for the decay chain (multiplicity = 1.03).

Background Sources

- Charged track combinatoric
- Mis-reconstructed π^0
- Real D^0 , fake π_s
- $K\pi\pi^0$ reflection in sideband



Event Selection

- $P_{\text{CM}}(D^0) > 2.77 \text{ GeV}/c$
- $|m_{D^{*+}} - m_{D^0} - 145.5| < 0.6 \text{ MeV}/c^2$

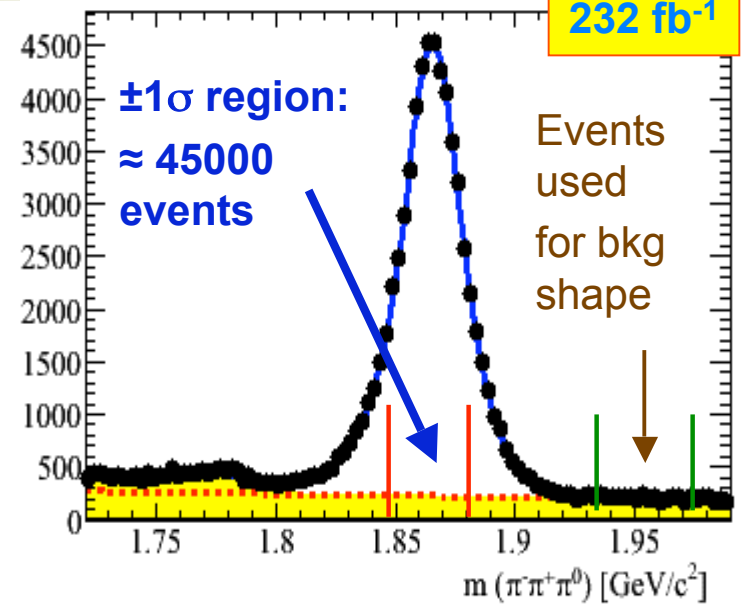
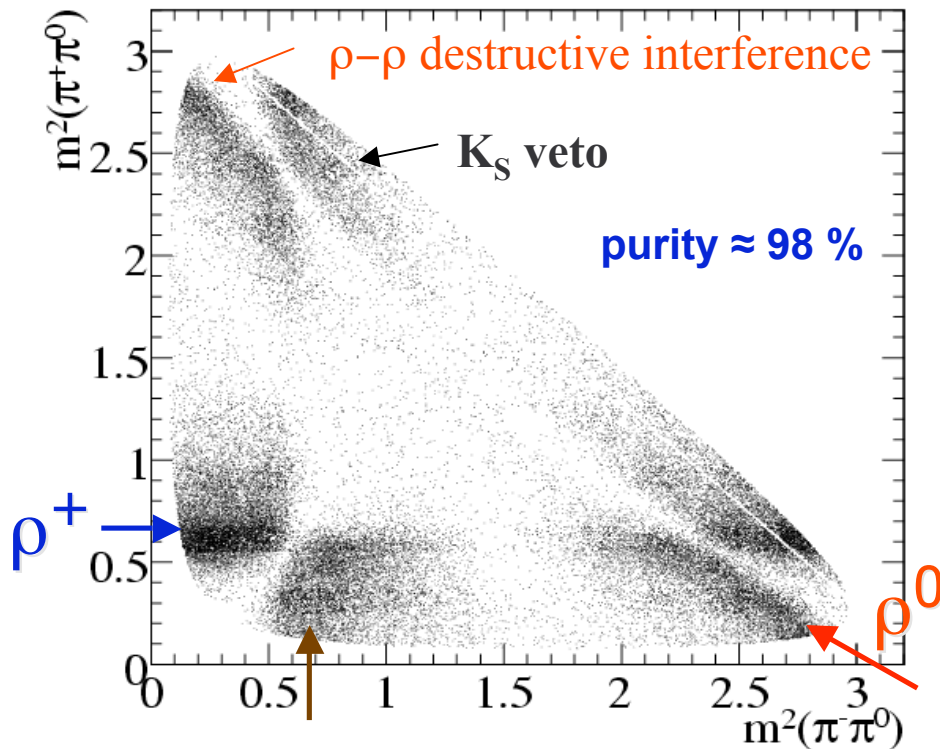
Phys. Rev. D74, 091102 (2006)

Step 1

Dalitz Plot Analysis of $D^0 \rightarrow \pi^- \pi^+ \pi^0$

Motivation: CKM angle γ using $B^\pm \rightarrow D[\rightarrow \pi^- \pi^+ \pi^0] K^\pm$

- Three $I=1$ particles in the final state
- Gives rise to a rich interference structure
- The three ρ regions are clearly enhanced in the DP, and ρ - ρ destructive interference is evident



The 3 destructively interfering $\rho\pi$ amplitudes suggest an $I = 0, \Delta I = 1/2$ dominated final state.
 C. Zemach, Phys. Rev. 133, B1201 (1964).

hep-ex / 0703037

Step 1

$D^0 \rightarrow \pi^- \pi^+ \pi^0$ Dalitz Plot Fit Results

ρ^+ : 68 %
 ρ^- : 35 %
 ρ^0 : 26 %

Small contributions from higher ρ , f_0 , f_2 and σ states

hep-ex/0703037

Systematic errors:

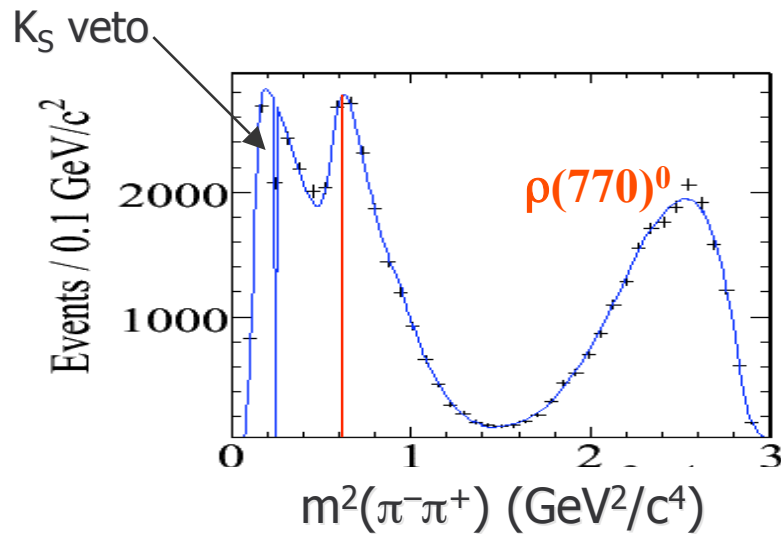
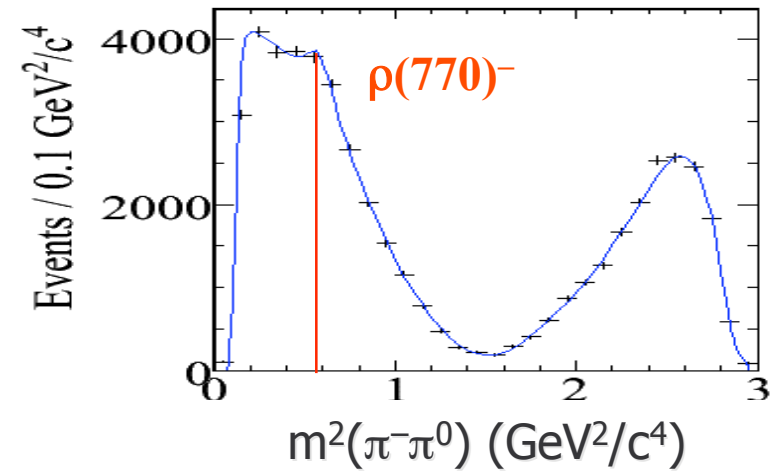
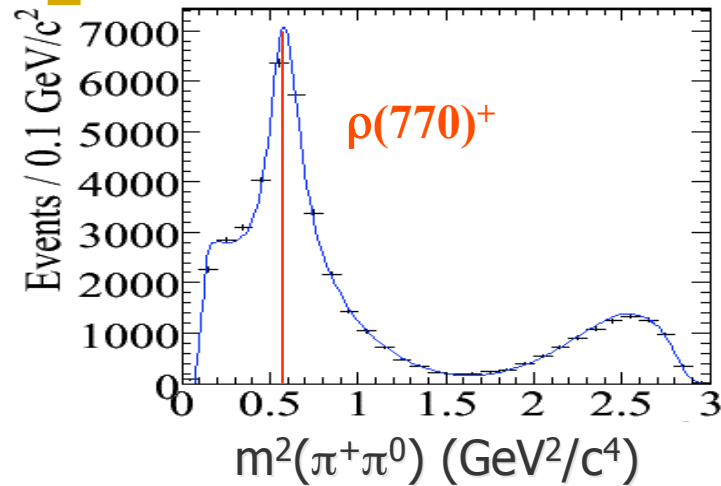
- σ and $\rho(1700)$ parameters
- reconstruction & PID eff
- Form factor variation
- Flavor mistags

The distribution is marked by 3 destructively interfering $\rho\pi$ amplitudes, suggesting an $I = 0$, $\Delta I = 1/2$ dominated final state.
 C. Zemach, Phys. Rev. 133, B1201 (1964).

State	Amplitude a_r	Phase ϕ_r	Fraction f_r (%)
$\rho^+(770)$	1	0	$67.8 \pm 0.0 \pm 0.2$
$\rho^0(770)$	$0.588 \pm 0.006 \pm 0.001$	$16.2 \pm 0.6 \pm 0.3$	$26.2 \pm 0.5 \pm 0.4$
$\rho^-(770)$	$0.714 \pm 0.008 \pm 0.003$	$-2.0 \pm 0.6 \pm 0.5$	$34.6 \pm 0.8 \pm 0.1$
$\rho^+(1450)$	$0.21 \pm 0.06 \pm 0.10$	$-146 \pm 18 \pm 8$	$0.11 \pm 0.07 \pm 0.06$
$\rho^0(1450)$	$0.33 \pm 0.06 \pm 0.04$	$10 \pm 8 \pm 6$	$0.30 \pm 0.11 \pm 0.07$
$\rho^-(1450)$	$0.82 \pm 0.05 \pm 0.04$	$16 \pm 3 \pm 3$	$1.79 \pm 0.22 \pm 0.12$
$\rho^+(1700)$	$2.25 \pm 0.18 \pm 0.14$	$-17 \pm 2 \pm 2$	$4.1 \pm 0.7 \pm 0.7$
$\rho^0(1700)$	$2.51 \pm 0.15 \pm 0.13$	$-17 \pm 2 \pm 2$	$5.0 \pm 0.6 \pm 0.9$
$\rho^-(1700)$	$2.00 \pm 0.11 \pm 0.07$	$-50 \pm 3 \pm 3$	$3.2 \pm 0.4 \pm 0.6$
$f_0(980)$	$0.052 \pm 0.004 \pm 0.006$	$-59 \pm 5 \pm 3$	$0.25 \pm 0.04 \pm 0.04$
$f_0(1370)$	$0.22 \pm 0.03 \pm 0.03$	$156 \pm 9 \pm 6$	$0.37 \pm 0.11 \pm 0.09$
$f_0(1500)$	$0.20 \pm 0.02 \pm 0.02$	$12 \pm 9 \pm 4$	$0.39 \pm 0.08 \pm 0.07$
$f_0(1710)$	$0.39 \pm 0.05 \pm 0.06$	$51 \pm 8 \pm 7$	$0.31 \pm 0.07 \pm 0.08$
$f_2(1270)$	$0.30 \pm 0.01 \pm 0.06$	$-171 \pm 3 \pm 2$	$1.32 \pm 0.08 \pm 0.08$
$\sigma(400, 600)$	$0.24 \pm 0.02 \pm 0.04$	$8 \pm 4 \pm 3$	$0.82 \pm 0.10 \pm 0.10$
Non-Res	$0.57 \pm 0.07 \pm 0.08$	$-11 \pm 4 \pm 2$	$0.84 \pm 0.21 \pm 0.12$

Step 1

$D^0 \rightarrow \pi^- \pi^+ \pi^0$ Dalitz Plot Fit Projections



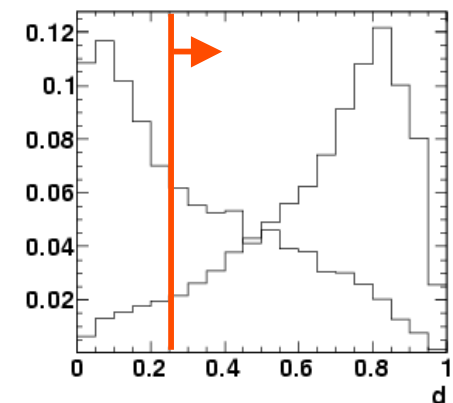
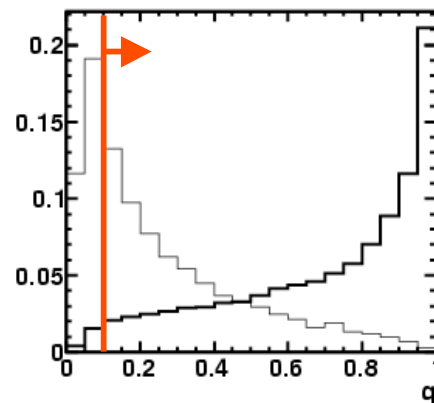
**Excellent agreement
between data & fit.**

Event Selection for $B^\pm \rightarrow D_{\pi^- \pi^+ \pi^0} K^\pm$

Based on BR and asymmetry analysis

Phys. Rev. D72, 071102 (2005)

- $5.272 < m_{ES} < 5.3$ GeV (Avoids DP- m_{ES} correlations in bkg)
- $1.83 < m_D < 1.895$ GeV (Avoids DP- m_D correlations in bkg)
- Kaon, pion identification
- $K_S \rightarrow \pi\pi$ veto ($D^0 \rightarrow K_S \pi^0$ is a CF decay unrelated to GGSZ method)
- $q > 0.1$ (continuum NN)
- $d > 0.25$ (fake D^0 NN)
- $\varepsilon = 11.4\%$ (efficiency)



Event Types in $B^\pm \rightarrow D_{\pi^- \pi^+ \pi^0} K^\pm$

1. DK_D : Correctly reconstructed signal (“signal”)
2. DK_{bgd} : Mis-reconstructed signal events
3. $D\pi_D$: Correctly-reconstructed $D\pi$ with π misidentified as K
4. $D\pi_{\text{badD}}$: $D\pi$ events with a fake D candidate. K candidate is usually a true kaon picked at random from the event
5. DKX : $B \rightarrow DK$ with $D \rightarrow \text{non-}\pi\pi\pi^0$. The K is good
6. $D\pi X$: $B \rightarrow D\pi/\rho$ with $D \rightarrow \text{non-}\pi\pi\pi^0$. K candidate is usually a true kaon picked at random from the event
7. BBC_D : Combinatoric BB events with a good D candidate
8. BBC_{badD} : Combinatoric BB events with a fake D candidate
9. qq_D : Continuum with a good D candidate
10. qq_{badD} : continuum with a fake D candidate

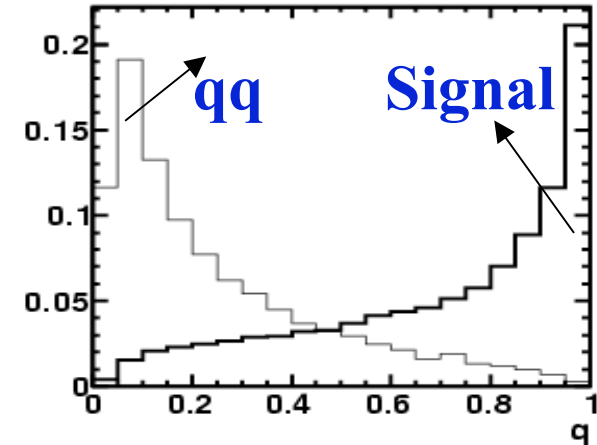
Step 2

BR & Asymmetry for $B^\pm \rightarrow D_{\pi^- \pi^+ \pi^0} K^\pm$

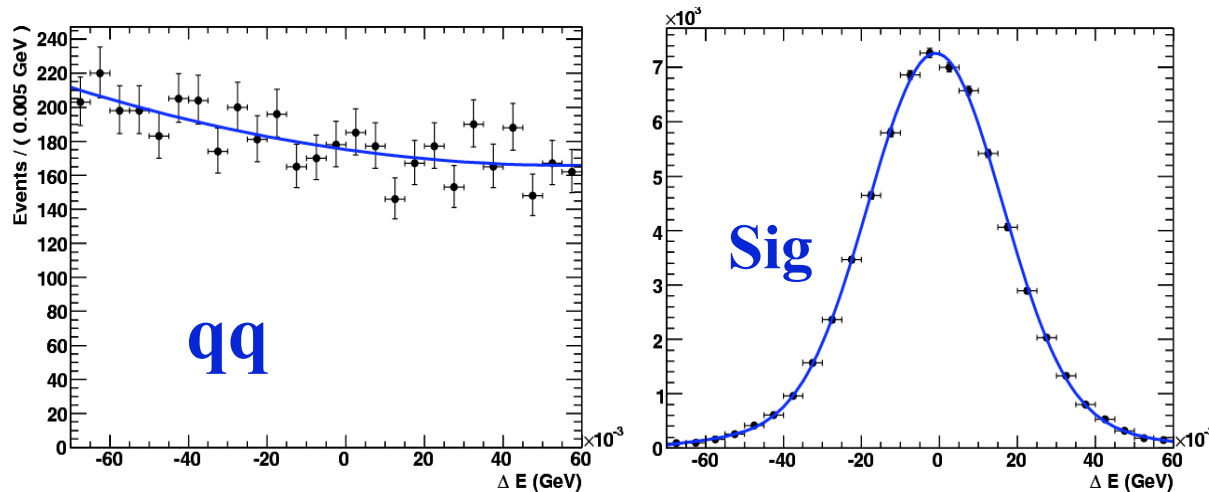
Fit $B^- \rightarrow D_{\pi\pi\pi^0} K^-$ sample with ΔE , q , d

Obtain signal yield & asymmetry

Nsig	170 ± 29
Asym	-0.02 ± 0.15



ΔE PDFs are Gaussian and 2nd-order polynomial:



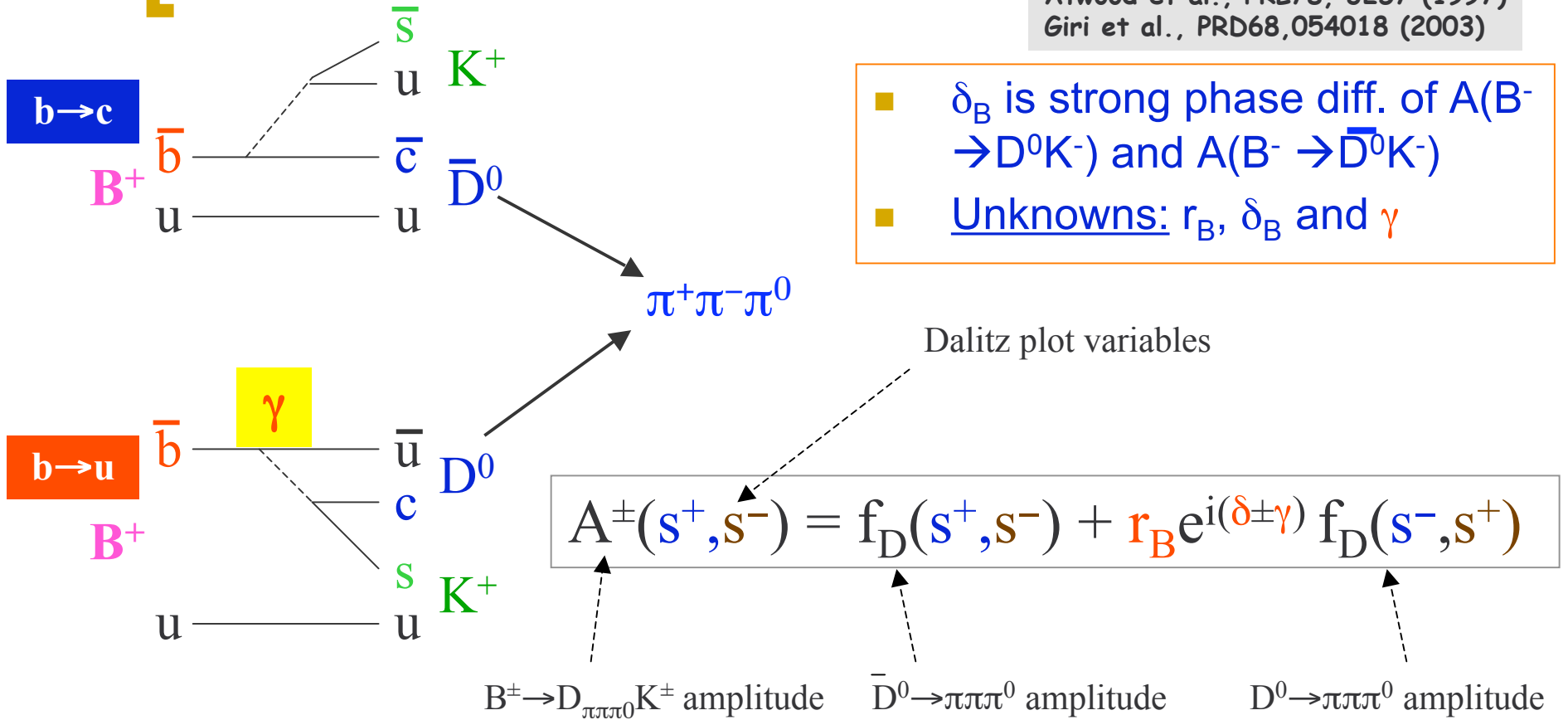
$$BR(B^- \rightarrow D_{\pi\pi\pi^0} K^-) = (4.6 \pm 0.8 \pm 0.7) \times 10^{-6}$$

$$A(B^- \rightarrow D_{\pi\pi\pi^0} K^-) = -0.02 \pm 0.15 \pm 0.03$$

Step 3

Extraction of γ : Basic Idea

Atwood et al., PRL78, 3257 (1997)
Giri et al., PRD68,054018 (2003)



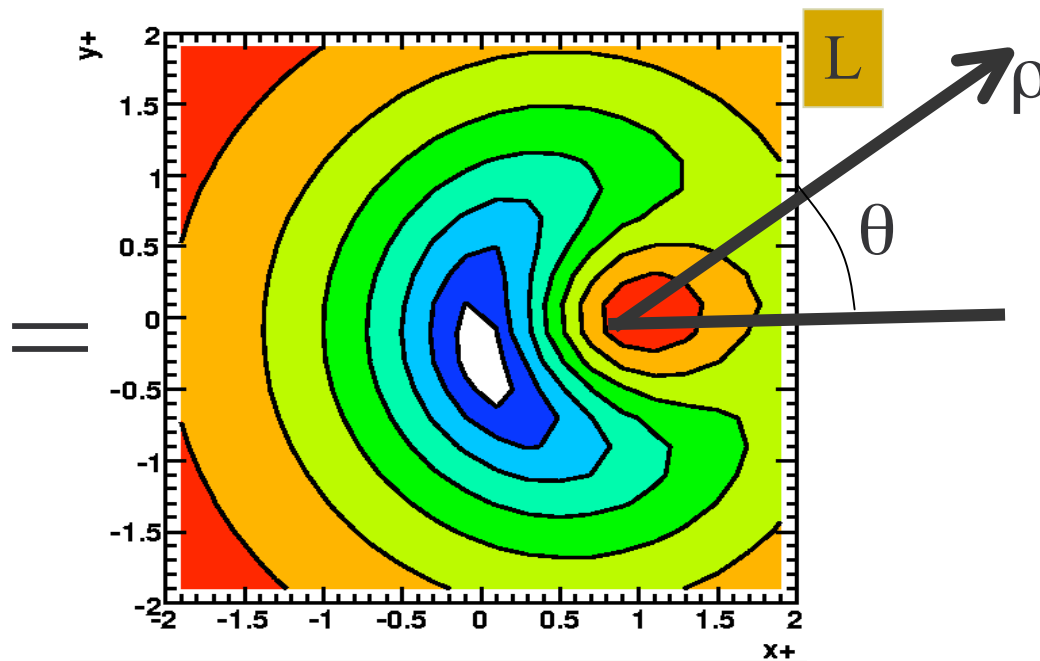
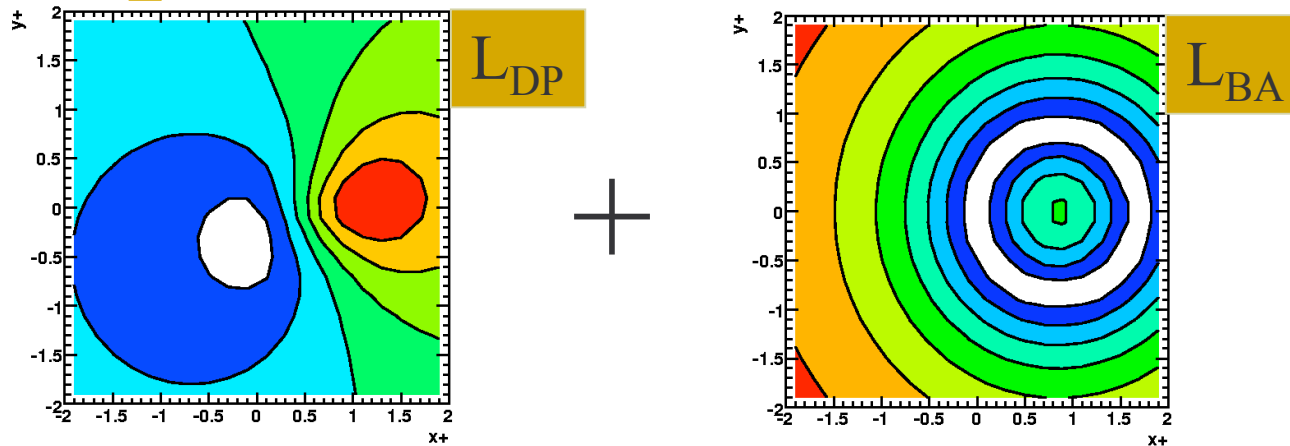
Based on GGSZ method of **PRD68, 054018**, so far used only with $D \rightarrow K_S \pi^+ \pi^-$

Add more Information to the Likelihood

- The Dalitz plot shape $|A^\pm(\mathbf{s}^+, \mathbf{s}^-)|^2$ depends on the CP parameters $r_B e^{i(\delta \pm \gamma)} = x_\pm + y_\pm$
 - Previous Dalitz analyses, with $K_S \pi^+ \pi^-$, used only this signature
- But the branching fractions $= \int |A^\pm(\mathbf{s}^+, \mathbf{s}^-)|^2$ are also sensitive to the CP parameters
 - Using both the shape and the absolute rates gives higher sensitivity
- It turns out that in this mode, the BRs give a higher sensitivity
 - Don't know how it is in $K_S \pi^+ \pi^-$ – need to check. If the same is true there, expect significant improvement in $K_S \pi^+ \pi^-$ sensitivity to γ

Step 3

Combined behavior $L = L_{DP} + L_{BA}$



- Highest sensitivity
- But correlated contours due to polar symmetry of L_{BA}
- Can't quote sensible errors
- Switch to polar coordinates

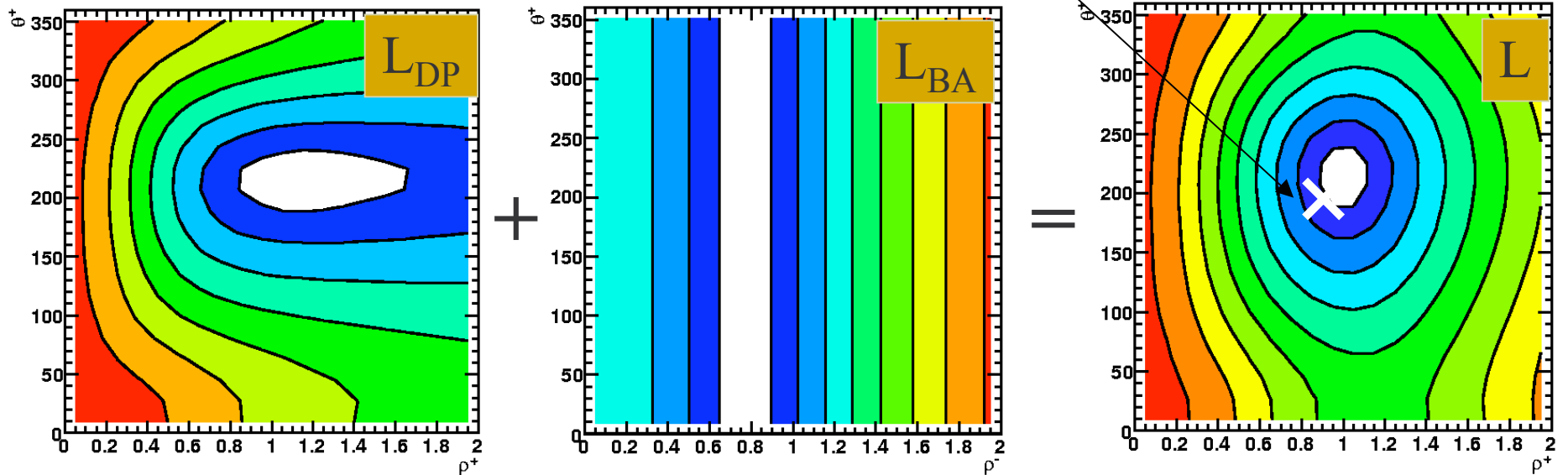
Step 3

Polar coordinates

$$\rho_{\pm} \equiv \sqrt{(x_{\pm} - x^0)^2 + y_{\pm}^2} \quad \theta_{\pm} \equiv \tan^{-1} \left(\frac{y_{\pm}}{x_{\pm} - x^0} \right)$$

$$x^0 = \int f_D(s^+, s^-) * f_D(s^-, s^+) ds^- ds^+ = 0.85$$

$\rho_{\pm} = x^0$ and $\theta = 180^\circ$ for $r_B = 0$ (no CP violation)



Step 3

Result with 344 M $e^+e^- \rightarrow B\bar{B}$ Events

$$r_B e^{i(\delta \pm \gamma)} = x_{\pm} + y_{\pm}$$

$$\rho_{\pm} \equiv \sqrt{(x_{\pm} - x^0)^2 + y_{\pm}^2}$$

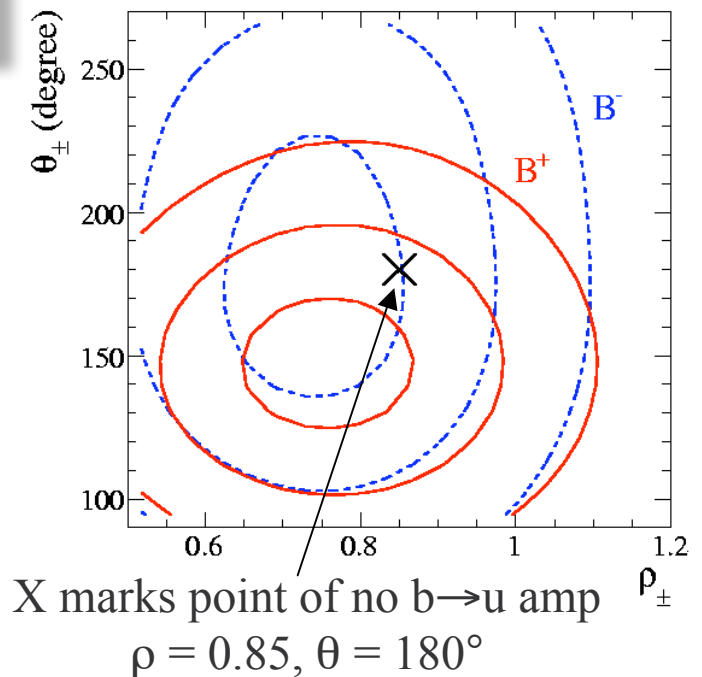
\downarrow
 $x^0 = 0.85$

$$\theta_{\pm} \equiv \tan^{-1} \left(\frac{y_{\pm}}{x_{\pm} - x^0} \right)$$

However, not trivial to directly determine γ

$$\begin{aligned} \rho^- &= 0.72 \pm 0.11 \pm 0.06 ; \\ \theta^- &= (173 \pm 42 \pm 16)^\circ \\ \rho^+ &= 0.75 \pm 0.11 \pm 0.06 ; \\ \theta^+ &= (147 \pm 23 \pm 11)^\circ \end{aligned}$$

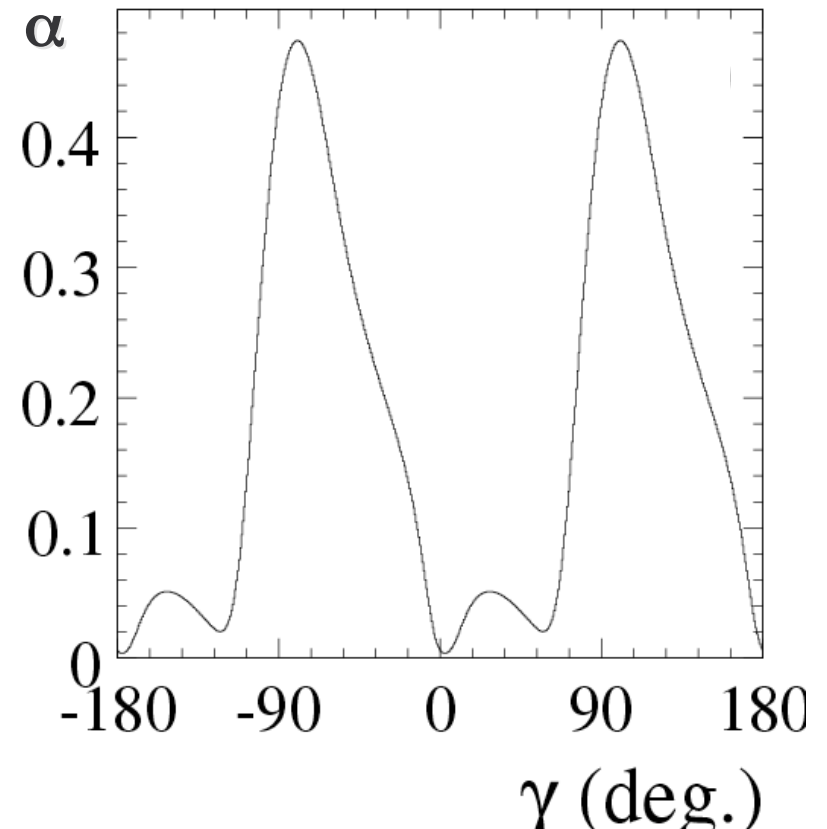
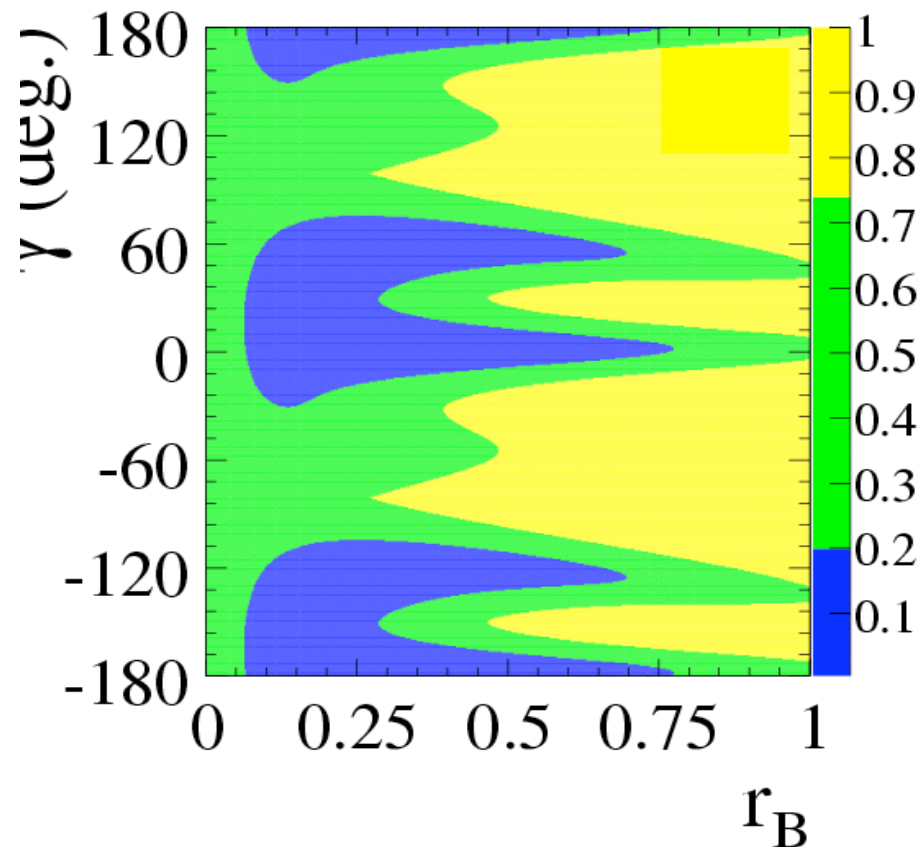
- First measurement of CP-violating quantities in $B \rightarrow D_{\pi\pi\pi^0} K$
- First combined use of DP distribution and absolute BR to extract CP parameters.
- σ_{θ} is too large for a meaningful extraction of γ from this analysis alone
- σ_{ρ} is small enough to contribute significantly to overall fits for γ



Step 3

From $(\rho_{\pm}, \theta_{\pm})$ to (r_B, δ, γ)

Use frequentist method to extract γ, r_B, δ from $(\rho_{\pm}, \theta_{\pm})$
(3dim confidence intervals projections)



1σ , 2σ , and 3σ regions are defined as containing the three-dimensional significance, α , smaller than 19.9 %, 73.9 %, and 97.1 %, respectively.

Step 3

Constraints on (r_B, δ, γ)

1σ bounds on the physical parameters, including both stat. and syst. errors

First direct lower bound on r_B

$$0.06 < r_B < 0.78$$

$$-30^\circ < \gamma < 76^\circ$$

$$-27^\circ < \theta < 78^\circ$$

[hep-ex / 0703037](#)

accepted for
publication in PRL

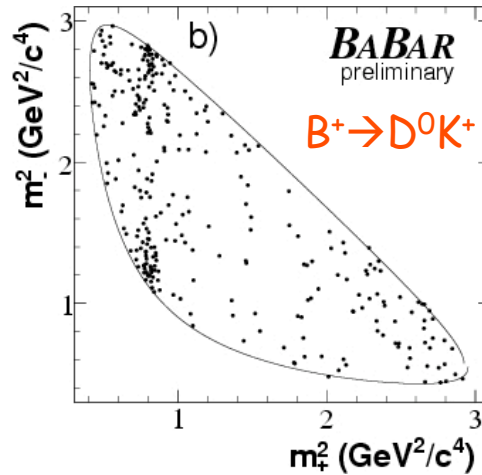
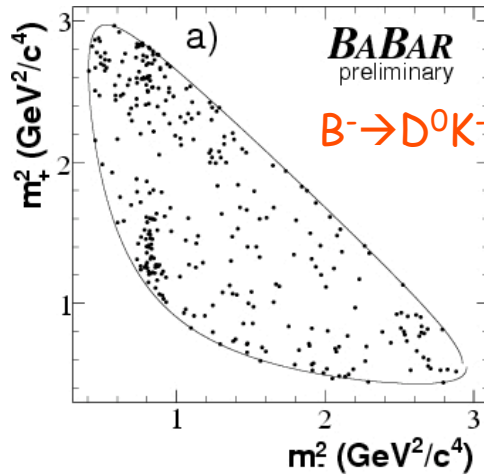
These bounds come from the results of this analysis alone.

Sensitivity to r_B , γ , and δ arises from the Dalitz plot and the BR asymmetry.

Hopefully, a more powerful bound will be obtained after combining the results of this analysis with those from $B^\pm \rightarrow D[-\rightarrow K_S^0 \pi^+ \pi^-] K^\pm$ analysis.

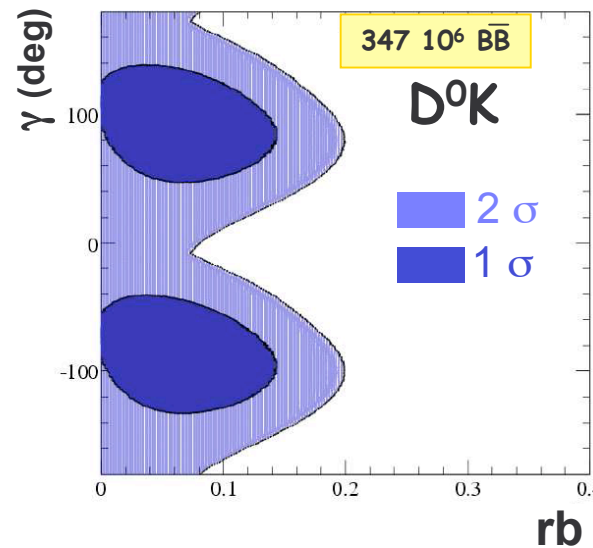
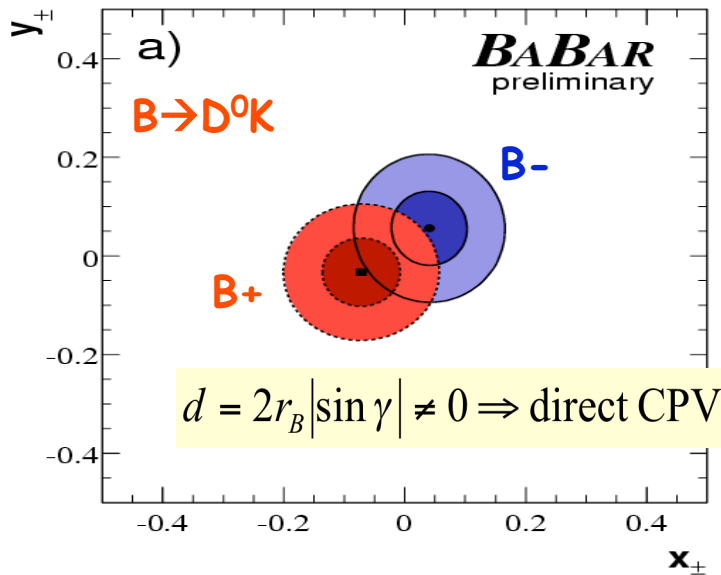
γ from $B^\pm \rightarrow D_{K_S^0 \pi^- \pi^+} K^\pm$

$D \rightarrow K_S \pi \pi$ Dalitz plot distribution in signal region



Used frequentist method to extract γ, r_B, δ_B from (x_\pm, y_\pm)

(x_\pm, y_\pm) are extracted from the $D^0 \rightarrow K_S \pi \pi$ Dalitz plot



$$r_B < 0.142 \quad (r_B < 0.198)$$

$$1\sigma \quad (2\sigma)$$

$$\gamma = (92 \pm 41 \pm 10 \pm 13)^\circ$$

(stat) (syst) (Dalitz)

(5dim confidence intervals projections)

hep-ex/0607104
hep-ex/0507101

[Summary

- Direct measurement of γ is crucial to constrain new physics contributions in quark sector of the Standard Model.
- Many different approaches to measure γ . Information from GLW, ADS, GGSZ, and other methods are all useful.
- The **GGSZ/Dalitz** method has emerged as the most powerful technique.
- Precise parameterizations of the amplitudes and phases and the inclusion of information on branching ratio and decay-rate asymmetry improve sensitivity in γ . A lot of progress made in the analysis and technique development.
- Statistics are the only thing holding us back ! Adding additional D decay modes to **B \rightarrow DK** and combining results from them will definitely help in the future analysis.

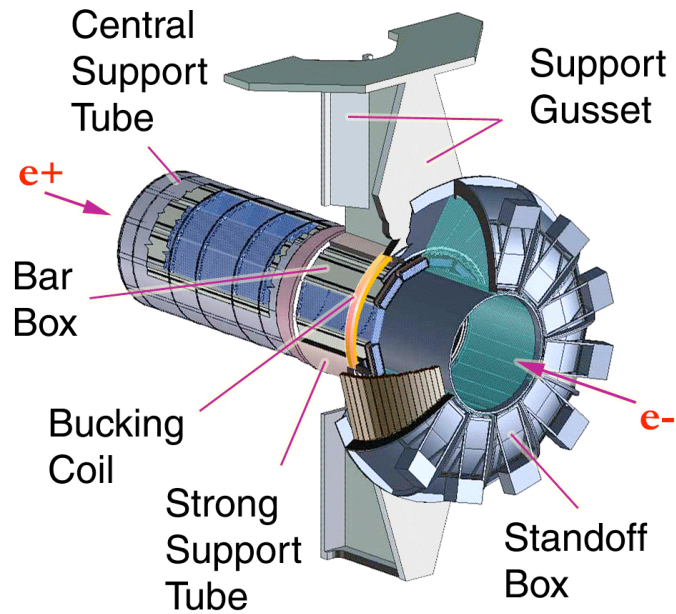
End of Talk ! Thank You !



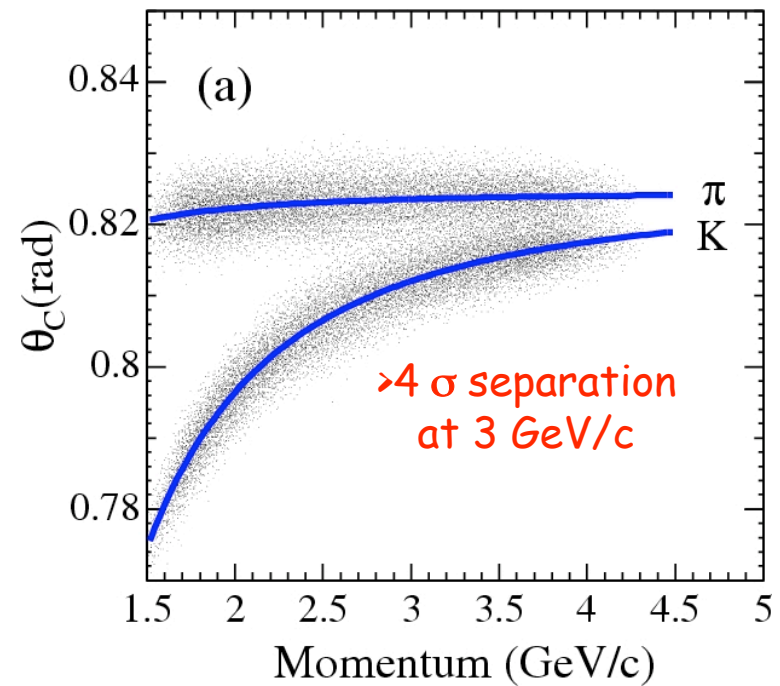
Back up slides

Kaon/Pion Discrimination: DIRC

LAYOUT



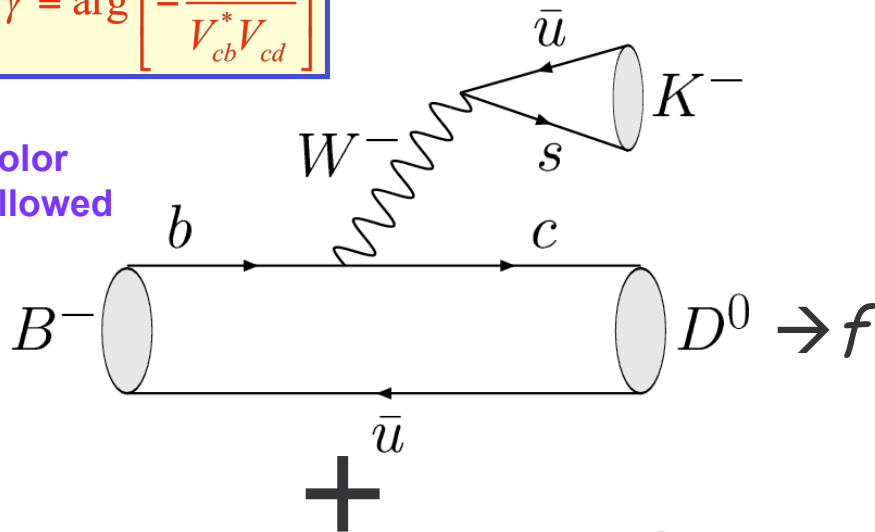
Cherenkov angle vs. momentum for pions and kaons



Methods to Extract γ

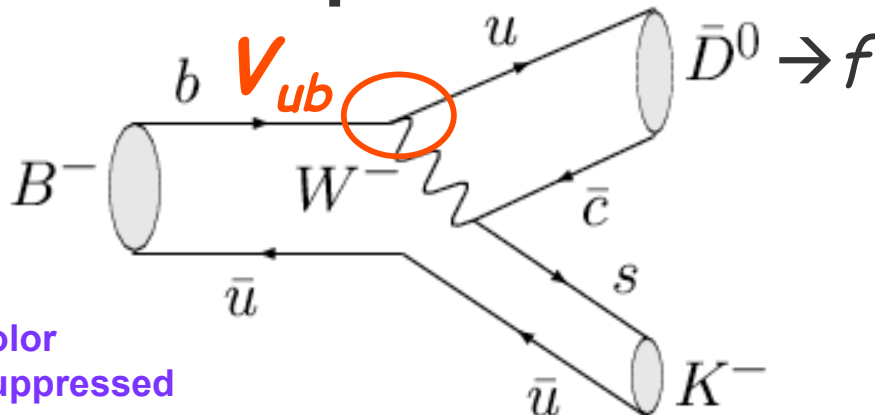
$$\gamma = \arg \left[-\frac{V_{ub}^* V_{ud}}{V_{cb}^* V_{cd}} \right]$$

color allowed



+

color suppressed



- D^0/\bar{D}^0 decay to common final state
- The interference depends on V_{ub} and therefore on γ
- Critical parameter: ratio of amplitudes:

$$r_B \equiv \left| \frac{A(B^- \rightarrow \bar{D}^0 K^-)}{A(B^- \rightarrow D^0 K^-)} \right| \sim 0.1$$

- Select the D^0 decays that enhance the interference:
 - 3-body (e.g. $K_S \pi \pi$): **Dalitz**
 - CP-eigen. (e.g. $K_S \pi^0$): **GLW**
 - DCS (e.g. $D^0 \rightarrow K^+ \pi^-$): **ADS**

γ measurements are overwhelmingly dominated by statistical errors.

Gronau-London-Wyler Method

- $B^- \rightarrow D_{CP}^0 K^{(*)-}$, where D_{CP}^0 is a CP -eigenstate decay
 (CP+: $D^0 \rightarrow \pi^+\pi^-, K^+K^-$ CP-: $D^0 \rightarrow K_S\pi^0$)

- We have the following observables:

$$R_{CP\pm} \equiv \frac{\Gamma(B^- \rightarrow D_{CP\pm}^0 K^-) + \Gamma(B^+ \rightarrow D_{CP\pm}^0 K^+)}{2\Gamma(B^- \rightarrow D^0 K^-)} = 1 \pm 2r_B \cos \gamma \cos \delta_B + r_B^2$$

Normalized to flavor state

$$A_{CP\pm} \equiv \frac{\Gamma(B^- \rightarrow D_{CP\pm}^0 K^-) - \Gamma(B^+ \rightarrow D_{CP\pm}^0 K^+)}{\Gamma(B^- \rightarrow D_{CP\pm}^0 K^-) + \Gamma(B^+ \rightarrow D_{CP\pm}^0 K^+)} = \pm 2r_B \sin \gamma \sin \delta_B / R_{CP\pm}$$

- 4 observables ($R_{CP+}, R_{CP-}, A_{CP+}, A_{CP-}$) \Rightarrow determine 3 unknowns (r_B, δ_B, γ)

$BF(B \rightarrow DK) \sim 10^{-4}$, $BF(D \rightarrow f_{CP}) \sim 10^{-2}$

Small... \Rightarrow strongly statistics limited

Gronau-London-Wyler Method Results: **BABAR**

$N_{BB}=214 \cdot 10^6$

$D_{CP}^0 K^-$

$$R_{CP+} = 0.87 \pm 0.14 \pm 0.06$$

$$A_{CP+} = 0.40 \pm 0.15 \pm 0.08$$

$$R_{CP-} = 0.80 \pm 0.14 \pm 0.08$$

$$A_{CP-} = 0.21 \pm 0.17 \pm 0.07 \quad A_{CP-} = -0.33 \pm 0.34 \pm 0.10 \cdot (+1.15 \pm 0.12)(A_{CP-} - A_{CP+})$$

$N_{BB}=123 \cdot 10^6$

$D^{*0} (D_{CP}^0 \pi^0) K^-$

$$R_{CP+} = 1.09 \pm 0.26^{+0.10}_{-0.08}$$

$$A_{CP+} = -0.02 \pm 0.24 \pm 0.05$$

Loose bound on r_B $R_{CP+} + R_{CP-} = 2(1 + r_B^2)$

More CP eigenstate final states still to be added...

$D_{CP}^0 K^{*-} (K^{*-} \rightarrow K_S \pi^-)$

$N_{BB}=227 \cdot 10^6$

$$R_{CP+} = 1.77 \pm 0.37 \pm 0.12$$

$$A_{CP+} = -0.09 \pm 0.20 \pm 0.06$$

$$R_{CP-} = 0.76 \pm 0.29 \pm 0.06^{+0.04}_{-0.14}$$

Additional systematic error on A_{CP-} (CP even background)

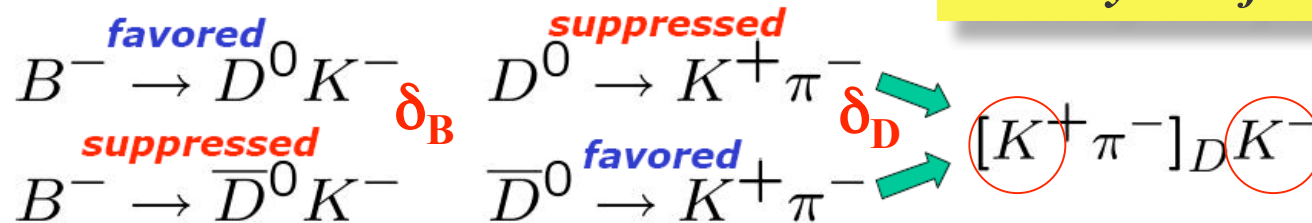
From $D_{CP} K^*$

$$r_B^2 = 0.23 \pm 0.24$$

More statistics needed to constrain γ

Atwood-Dunietz-Soni Method

D decay into flavor state



Count B candidates with opposite sign kaons

$$R_{ADS} = \frac{Br([K^+ \pi^-]K^-) + Br([K^- \pi^+]K^+)}{Br([K^- \pi^+]K^-) + Br([K^+ \pi^-]K^+)} = r_D^2 + r_B^2 + 2r_B r_D \cos(\delta_D + \delta_B) \cos \gamma$$

$$A_{ADS} = \frac{Br([K^+ \pi^-]K^-) - Br([K^- \pi^+]K^+)}{Br([K^+ \pi^-]K^-) + Br([K^- \pi^+]K^+)} = 2r_B r_D \sin(\delta_D + \delta_B) \sin \gamma / R_{ADS}$$

$$\text{Input: } r_D = \frac{|A(D^0 \rightarrow K^+ \pi^-)|}{|A(D^0 \rightarrow K^- \pi^+)|} = 0.060 \pm 0.003$$

D decay strong phase δ_D unknown

No significant signal in current dataset

Dalitz Plot Method

- We saw that at least 2 D final states are needed in order to solve for all the unknowns.
- This 2-state requirement can be satisfied by a single multi-body D final states, in which each point in the final state phase space (Dalitz plot for a 3-body decay) serves effectively as a different final state.
- In terms of the γ analysis, what differentiates 2 final states is their values of r_f and/or δ_f . In this sense, different points in phase space can function as different D final states when they have different values of r_f or δ_f .
- Broad resonances are the most obvious cause for variation of r_f and δ_f in different points of final-state phase space.

Assessment of Some 3-body D^0 Decays

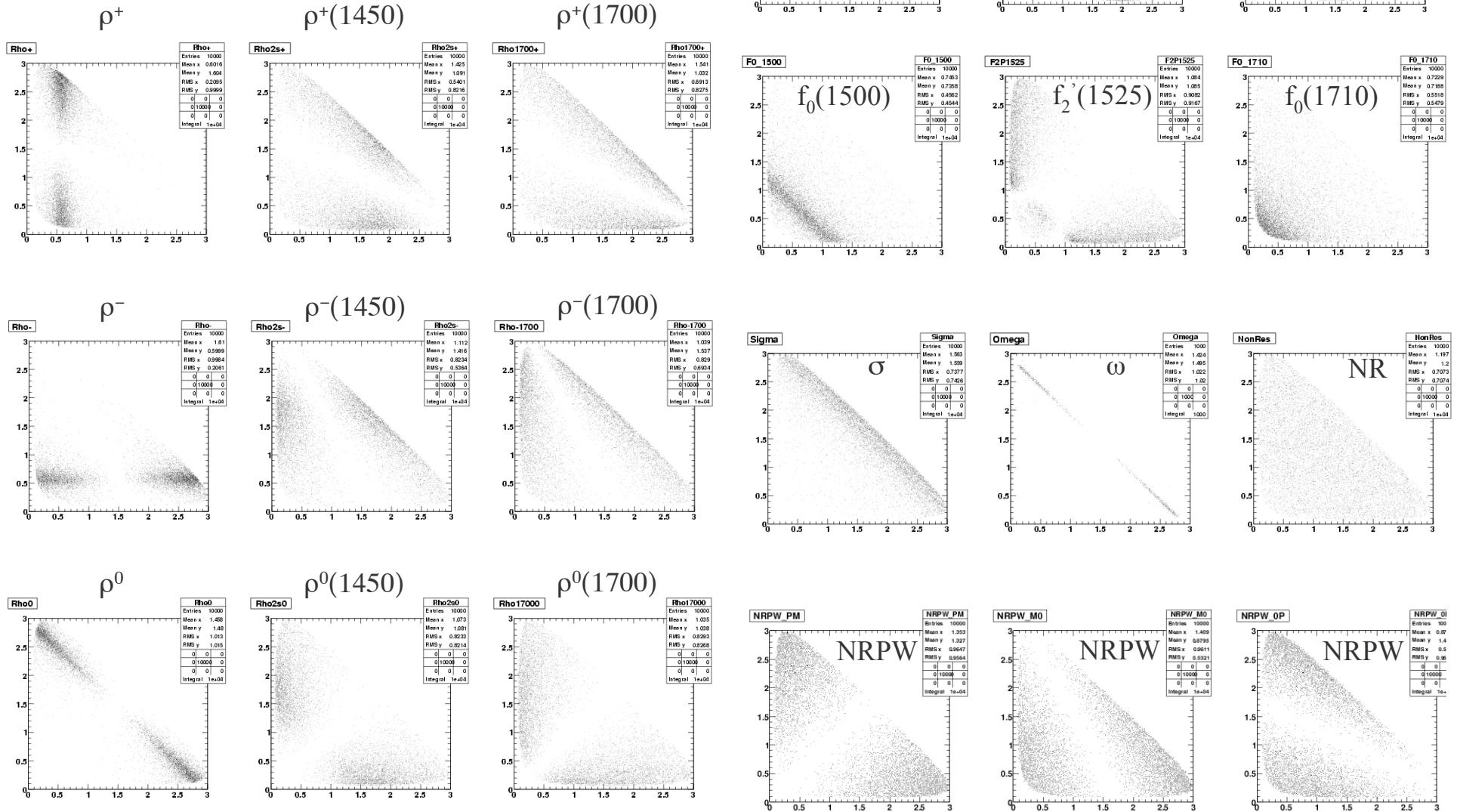
Mode	BR($D^0 \rightarrow f$)	λ^n	$ A(\overline{D^0})/A(D^0) $	Bgd	Comments
$K_S \pi^+ \pi^-$	2.9%	n=0	$\sim \lambda^2$ to 1	OK	Attractive due to high stat & low background
$\pi^+ \pi^- \pi^0$	1.5%	n=1	~ 1	π^0	Expect similar sensitivity as $K_S \pi \pi$ if background under control
$K_S K^+ \pi^-$	(0.34 \oplus 0.26)%	n=1	~ 1	OK	Expect similar sensitivity as $\pi \pi \pi^0$
$K^+ \pi^- \pi^0$	$\sim 0.2\%$	n=2	$\sim 1/\lambda^2$	π^0	S/B probably too small for now
$K^+ K^- \pi^0$	0.3%	n=1	~ 1	π^0 bad, KK good	Low stat, but low background, so sensitivity could approach $\pi \pi \pi^0$
$K_S \pi^0 \pi^0$	$\sim 1\%$ (+?)	n=0	1	$2\pi^0$	CP eigenstate, low S/B
$K_S \pi^+ \pi^- \pi^0$	5.5%	n=0	$\sim \lambda^2$	So-so	High stat, but 4-body analysis is hard. Large phase space reduces D^0 - D^0 bar interference

Analysis with Multi-body D^0 Final States

1. The simplest extension of the 2-body analysis.
2. Divide phase space into small bins, so that variations of r_f and δ_f within each bin can be ignored. Distant bins will have values of r_f and δ_f that are different enough so as to constitute different final states, and the analysis can be carried out, in principle, with as few as 2 bins.
3. A more accurate solution is not to ignore the variations of r_f and δ_f over the bin. But this introduces a new unknown for each bin. We now have 3 unknowns - r_f , $\sin \delta_f$, and $\cos \delta_f$. The analysis then requires a minimum of 4 bins.
4. The only approach carried out so far is to parameterize the continuous variation of r_f and δ_f over phase space by using a sum of interfering Breit-Wigner resonances.

Step 1

Signal Dalitz PDFs



Step 1

Strong-phase Diff. & Amplitude Ratio

- The strong phase difference δ_D and relative amplitude r_D between the decays of D^0 and D^0 to $\rho(770)^+ \pi^-$ state are defined, neglecting direct CP violation in D decays, by the equation:

$$r_D e^{i\delta_D} = \frac{a_{D^0 \rightarrow \rho^- \pi^+}}{a_{D^0 \rightarrow \rho^+ \pi^-}} e^{i(\delta_{\rho^- \pi^+} - \delta_{\rho^+ \pi^-})}$$

- We find

BaBar

Cleo

$$r_D = 0.714 \pm 0.008 \text{ (stat)} \pm 0.003 \text{ (syst)}$$

$$\delta_D = -2.0^\circ \text{ (stat)} \pm 0.6^\circ \pm 0.6^\circ \text{ (syst)}$$

$$r_D = 0.65 \pm 0.03 \text{ (stat)} \pm 0.04 \text{ (syst)}$$

$$\delta_D = -4^\circ \pm 3^\circ \text{ (stat)} \pm 4^\circ \text{ (syst)}$$

Hep-ex / 0703037 (2007)

Hep-ex / 0306048 (2003)

These measurements are consistent with each other.

Step 1

Introducing Angular Moments

Schrödinger's Equation

$$-\frac{\hbar^2}{2\mu} \nabla^2 \Psi(\vec{r}) + V(\vec{r})\Psi(\vec{r}) = E\Psi(\vec{r})$$

$$\left\{ \begin{array}{l} V(\vec{r}) = 0 \\ \vec{k} = \frac{\vec{p}}{\hbar} = \mu \frac{\vec{v}}{\hbar} \quad \mu = \frac{m_1 m_2}{m_1 + m_2} \end{array} \right.$$

$$|i\rangle = \Psi_i = \sum_{l=0}^{\infty} U_l(r) P_l(\cos \vartheta)$$

$$\Psi_S = \Psi_f - \Psi_i = \frac{1}{k} \sum_{l=0}^{\infty} (2l+1) \frac{\eta_l e^{2i\delta_l} - 1}{2i} P_l(\cos \vartheta) \frac{e^{ikr}}{r}$$

Angular Amplitude

Dynamic Amplitude
(BW, Flatte, S-wave)

In case only $l = 0$ (S-wave) and $l = 1$ (P-wave) amplitudes are present :

$$\left\{ \begin{array}{l} \sqrt{4\pi} \langle Y_0^0 \rangle = S^2 + P^2 \\ \sqrt{4\pi} \langle Y_1^0 \rangle = 2|S||P| \cos \phi_{SP} \\ \sqrt{4\pi} \langle Y_2^0 \rangle = \frac{2}{\sqrt{5}} P^2 \end{array} \right.$$

For S- and P- waves only, in the absence of cross-feeds from other channels, the amplitudes and the relative phase are given by:

We cannot solve these Eqs for the $\pi\pi$ system (due to crossfeeds) to extract $|S|$, $|P|$, and $\cos \phi_{SP}$ in a model independent way.

Step 2

BR & Asymmetry for $B^\pm \rightarrow D_{\pi^- \pi^+ \pi^0} K^\pm$

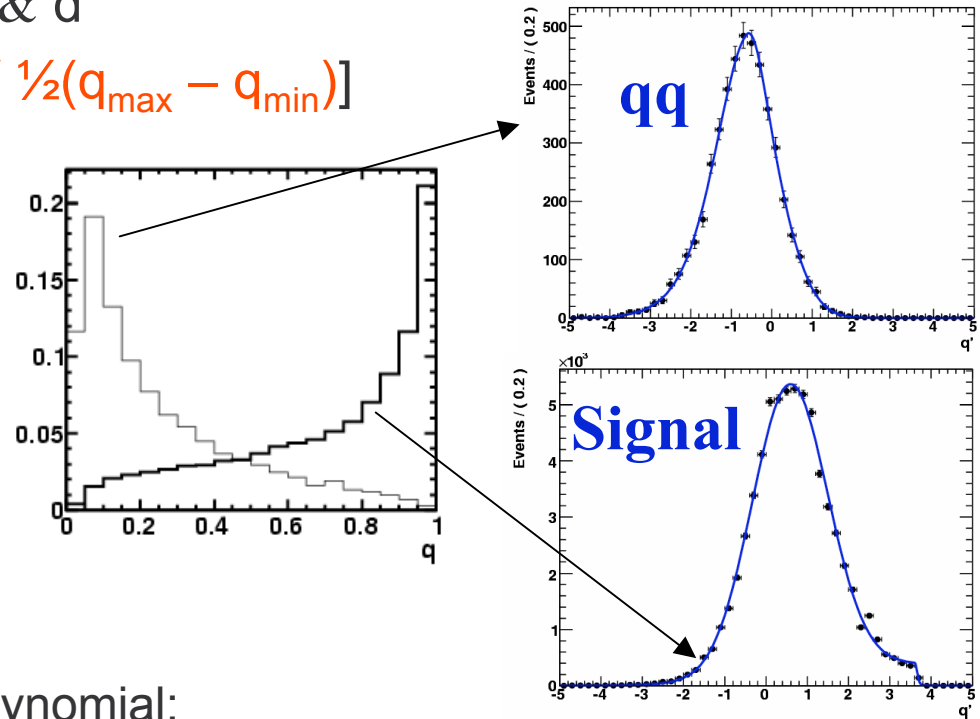
“Normalize” neural net variables q & d

$$q \rightarrow q' = \tanh^{-1}[(q - \frac{1}{2}(q_{\max} + q_{\min})) / \frac{1}{2}(q_{\max} - q_{\min})]$$

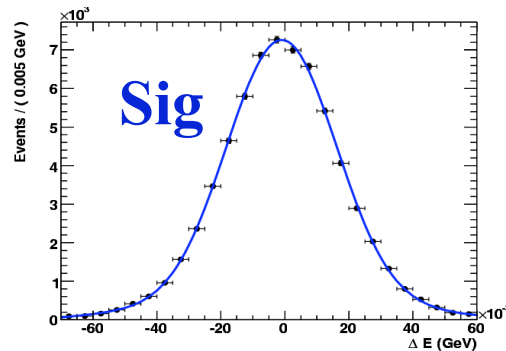
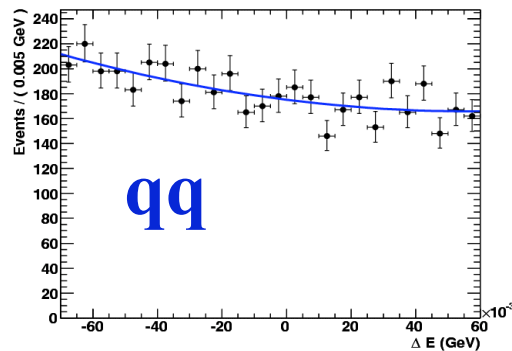
Fit $B^- \rightarrow D_{\pi\pi\pi^0} K^-$ sample with ΔE , q , d

Obtain signal yield & asymmetry

Nsig	170 ± 29
Asym	-0.02 ± 0.15



ΔE PDFs are Gaussian and 2nd-order polynomial:



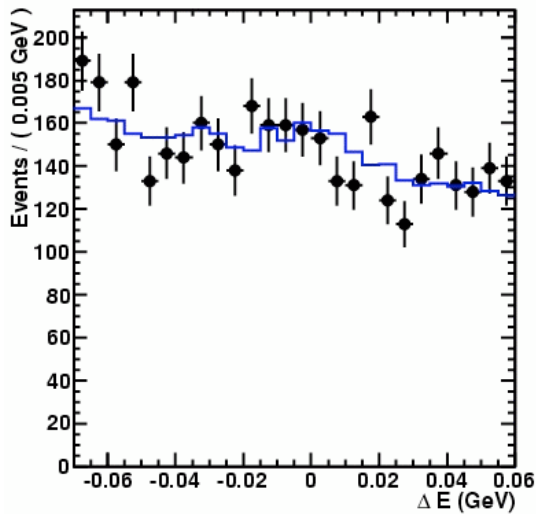
$$BR(B^- \rightarrow D_{\pi\pi\pi^0} K^-) = (4.6 \pm 0.8 \pm 0.7) \times 10^{-6}$$

$$A(B^- \rightarrow D_{\pi\pi\pi^0} K^-) = -0.02 \pm 0.15 \pm 0.03$$

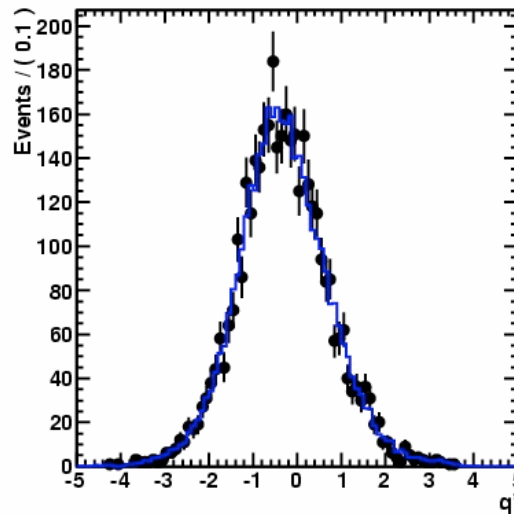
Step 2

BR of $B^\pm \rightarrow D_{\pi^- \pi^+ \pi^0} K^\pm$: Fit Projections

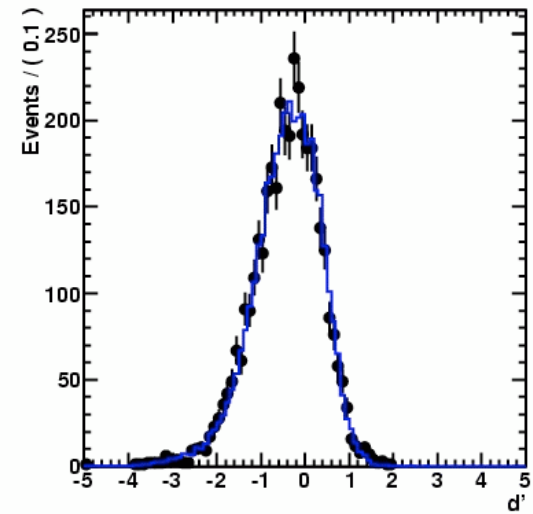
ΔE projection



q' projection



d' projection



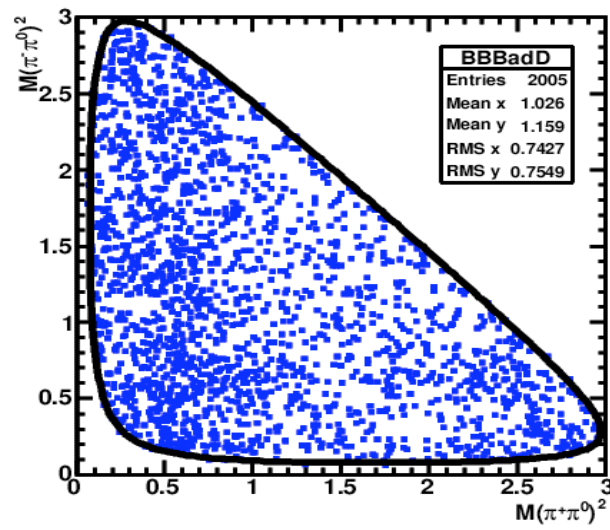
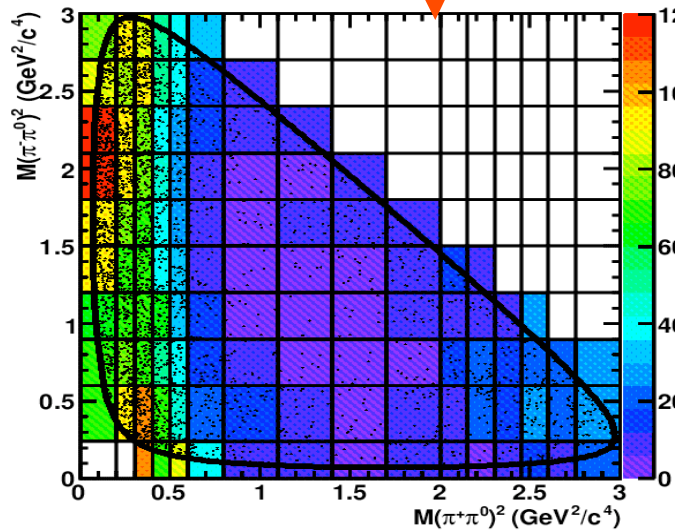
Nsig	170 ± 29
Asym	-0.02 ± 0.15
$N_{BB \text{ fake } D}$	1138 ± 76
$N_{qq \text{ fake } D}$	2383 ± 71
$N_{D\pi}$	57 ± 20
$N_{D\pi X} / N_{BB}$	0.53 ± 0.15

$\rightarrow \text{BR}(B^- \rightarrow D_{\pi\pi\pi^0} K^-) = (4.6 \pm 0.8 \pm 0.7) \times 10^{-6}$

Step 3

$B^\pm \rightarrow D_{\pi^- \pi^+ \pi^0} K^\pm$: Bkg Dalitz Shapes

- Fake-D background Dalitz shapes are NR + 3 incoherent, unpolarized ρ 's:
- Shape for 2 event types can't be fit to this way. We use an empirical shape from simulation:



For CP Fit

- Fit $D^0 \rightarrow \pi^+ \pi^- \pi^0$ Dalitz plot from $B^- \rightarrow D_{\pi\pi\pi^0} K^-$ sample with ΔE , q , s^+ , s^-
- NN variable d not used – highly correlated with s^+ , s^-
- m_{ES} and M_D not used – correlated with other variables for the background

CP Parameters: Max Likelihood Fit

- To make use of both the shape and the absolute decay rates, we minimize the function

$$L = L_{DP} + L_{BA}$$

$$L_{DP} = -\log \prod P_{DP}$$

$$L_{BA} = \frac{1}{2} Y_i V_{ij}^{-1} Y_j$$

$$Y = \begin{pmatrix} N_{\text{meas}} - N_{\text{expected}} \\ \text{Asym}_{\text{meas}} - \text{Asym}_{\text{expected}} \end{pmatrix}$$

V = error matrix from N and Asym fit

$$N_{\text{expected}}^{\pm} = \eta \int |A^{\pm}(s^+, s^-)|^2 \epsilon(s^+, s^-) / \int |f_D(s^+, s^-)|^2 \epsilon(s^+, s^-)$$

$$\underbrace{\hspace{15em}}_{1/2 N_{BB} \epsilon \text{BR}(D^0 \rightarrow \pi\pi\pi^0) \text{BR}(B^- \rightarrow D^0 K^-)}$$

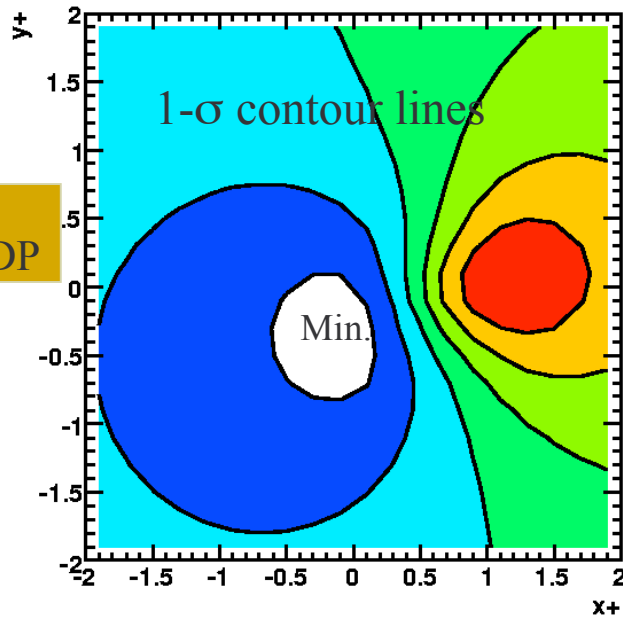
Step 3

Behavior of L_{DP} & L_{BA} for $x_{\text{true}} = y_{\text{true}} = 0$

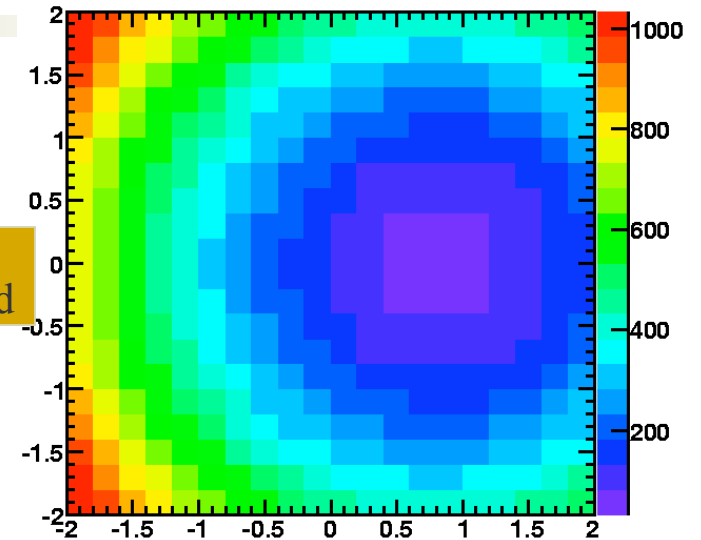
$$r_B e^{i(\delta \pm \gamma)} = x_{\pm} + y_{\pm}$$

Toy exp., S+B

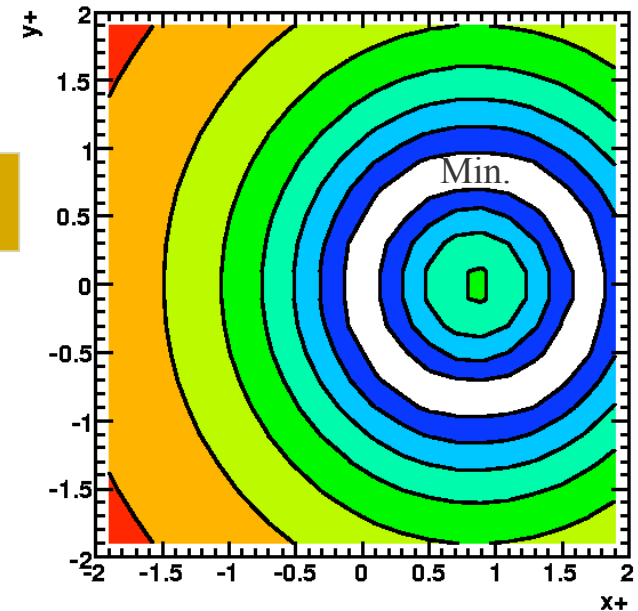
L_{DP}



N^+ expected



L_{BA}

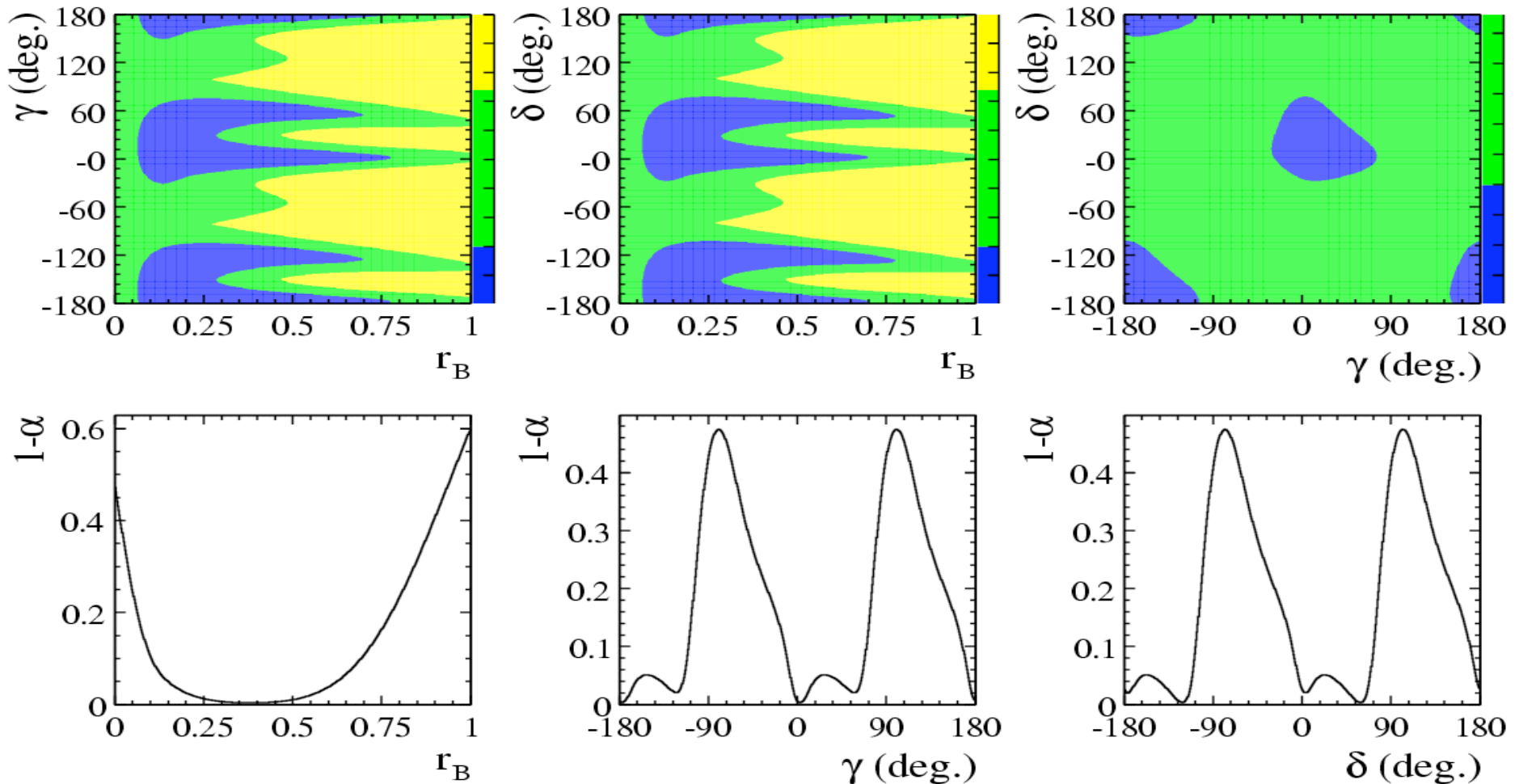


- L_{DP} (L_{BA}) has Cartesian (polar) symmetry
- L_{BA} is more sensitive (denser contour lines) in radial direction (ρ), not sensitive at all in θ

Step 3

From $(\rho_{\pm}, \theta_{\pm})$ to (r_B, δ, γ)

Use frequentist method to extract γ, r_B, δ_B from $(\rho_{\pm}, \theta_{\pm})$
(3dim confidence intervals projections)



Systematics details

■ Dalitz Model:

Dalitz model	ρ_-	θ_-	ρ_+	θ_+
NR _S , $\rho(770)$	0.0633	17.70	0.0359	-7.30
+ $f_0(980)$	0.0583	22.86	0.0260	4.63
+ $\rho(1450)$	0.0010	7.20	-0.0138	-8.50
+ $\rho(1700)$	0.0248	4.12	0.0043	-10.46
+ $f_0(1370, 1500, 1710), f_2(1270)$	-0.0249	-11.89	-0.0287	-1.67
+ σ	0	0	0	0
+ NR _P	0.0106	-0.23	0.0086	-1.46
+ $\omega, f_2'(1525)$	0.0091	2.66	0.0077	-2.07
$R = 0$	0.0017	-8.56	0.0005	-0.09

■ BR:

Source	BF error (%)	Section
PID efficiency	3.1	13.12
π^0 efficiency	3.0	13.16
Tracking efficiency	1.5	13.17
B counting	1.1	13.18
Total	4.70	

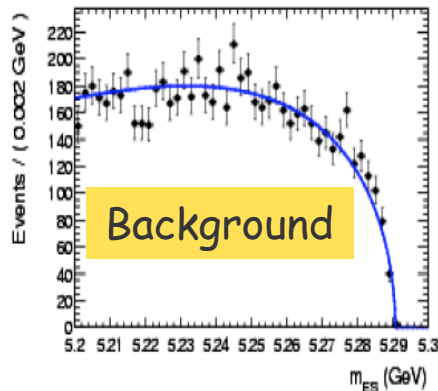
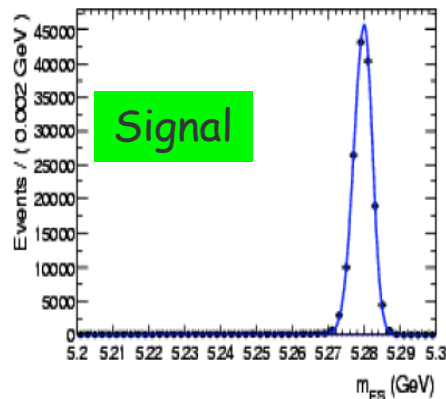
■ CP systematics

Source	ρ_-	θ_-	ρ_+	θ_+	Section
$\mathcal{B}(B^- \rightarrow D^0 K^-)$	0.0288	1.56	0.0277	1.05	13.19
$\mathcal{B}(D^0 \rightarrow K^- \pi^+ \pi^0)$	0.0174	0.88	0.0167	0.66	13.19
$\frac{\mathcal{B}(D^0 \rightarrow \pi^+ \pi^- \pi^0)}{\mathcal{B}(D^0 \rightarrow K^- \pi^+ \pi^0)}$	0.0058	0.01	0.0056	0.01	13.19
Signal efficiency	0.0148	0.02	0.0141	0.03	13.19
$N_{B\bar{B}}$	0.0049	0.01	0.0046	0.01	13.19
Total	0.0375	1.79	0.0360	1.24	

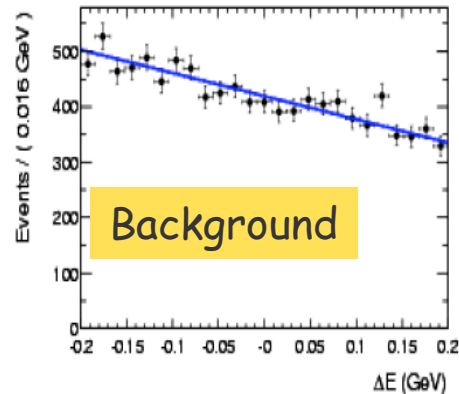
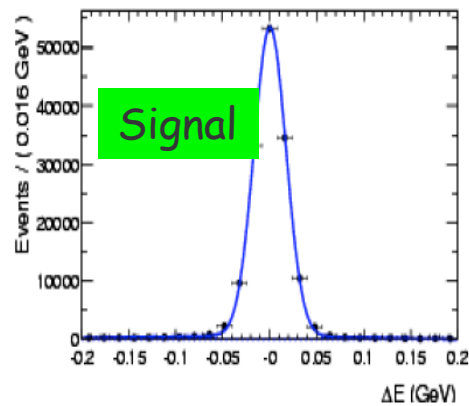
γ : Key Analysis Technique

Exploit kinematics of $e^+e^- \rightarrow \Upsilon(4S) \rightarrow B\bar{B}$ for signal selection

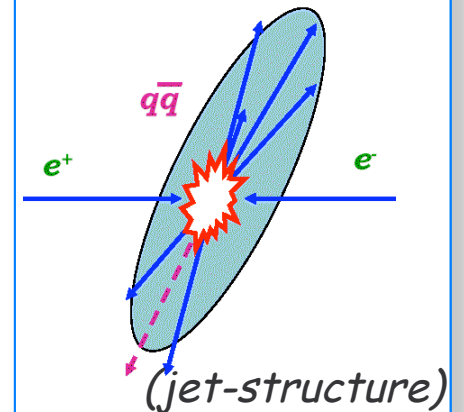
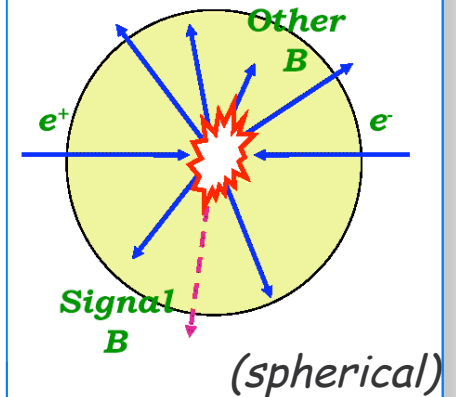
$$m_{ES} = \sqrt{E_{beam}^{*2} - p_B^{*2}}$$



$$\Delta E = E_B^* - E_{beam}^*$$



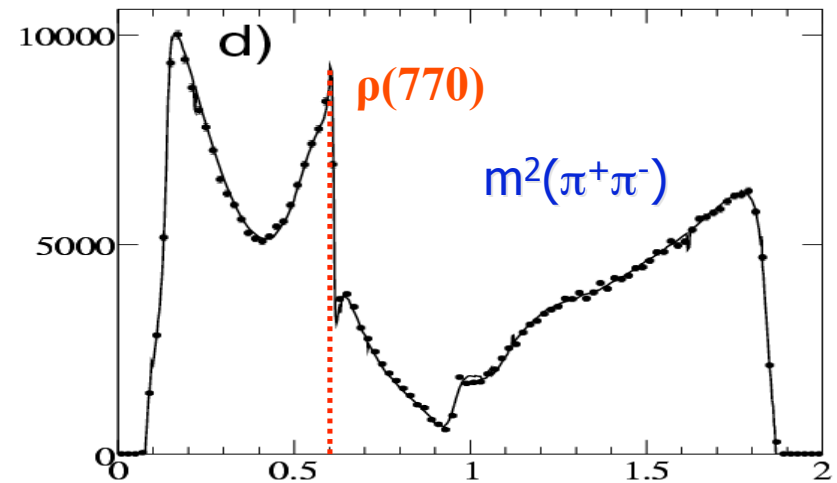
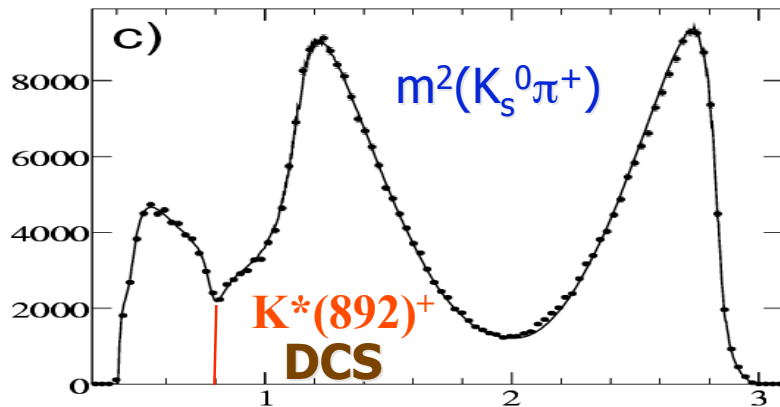
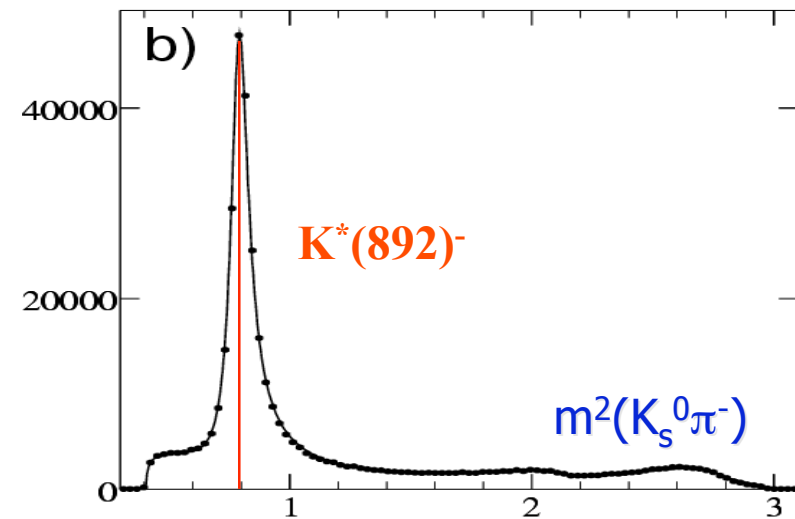
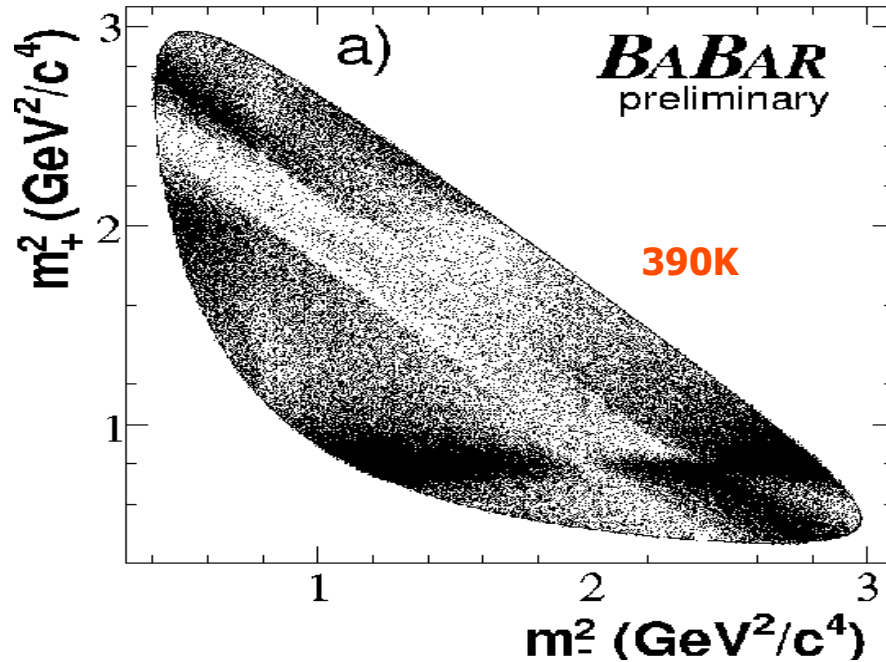
Event topology



$D^0 \rightarrow K_S^0 \pi^+ \pi^-$ Dalitz Plot analysis

Motivation: CKM angle γ using $B \rightarrow D[K_S^0 \pi^+ \pi^-] K^-$ decay

270 fb⁻¹



$D^0 \rightarrow K_S^0 \pi^+ \pi^-$ (Isobar Model)



Component	$Re\{a_r e^{i\phi_r}\}$	$Im\{a_r e^{i\phi_r}\}$	Fit fraction (%)
$K^*(892)^-$	-1.223 ± 0.011	1.3461 ± 0.0096	58.1
$K_0^*(1430)^-$	-1.698 ± 0.022	-0.576 ± 0.024	6.7
$K_2^*(1430)^-$	-0.834 ± 0.021	0.931 ± 0.022	3.6
$K^*(1410)^-$	-0.248 ± 0.038	-0.108 ± 0.031	0.1
$K^*(1680)^-$	-1.285 ± 0.014	0.205 ± 0.013	0.6
$K^*(892)^+$ <small>DCS</small>	0.0997 ± 0.0036	-0.1271 ± 0.0034	0.5
$K_0^*(1430)^+$ <small>DCS</small>	-0.027 ± 0.016	-0.076 ± 0.017	0.0
$K_2^*(1430)^+$ <small>DCS</small>	0.019 ± 0.017	0.177 ± 0.018	0.1
$\rho(770)$	1	0	21.6
$\omega(782)$	-0.02194 ± 0.00099	0.03942 ± 0.00066	0.7
$f_2(1270)$	-0.699 ± 0.018	0.387 ± 0.018	2.1
$\rho(1450)$	0.253 ± 0.038	0.036 ± 0.055	0.1
Non-resonant	-0.99 ± 0.19	3.82 ± 0.13	8.5
$f_0(980)$	0.4465 ± 0.0057	0.2572 ± 0.0081	6.4
$f_0(1370)$	0.95 ± 0.11	-1.619 ± 0.011	2.0
$\sigma(490, 406)$	1.28 ± 0.02	0.273 ± 0.024	7.6
$\sigma'(1024, 89)$	0.290 ± 0.010	-0.0655 ± 0.0098	0.9

$K^*(892)^- : 58 \%$
 $\rho(770)^0 : 22 \%$
 Non-Res.: 8 %
 $\sigma(500) : 8 \%$
 $K^*(1430)^- : 7 \%$
 $f_0(980) : 6 \%$

← Important for γ and D-mixing measurements

[hep-ex/0607104](https://arxiv.org/abs/hep-ex/0607104)

The 'Cartesian coordinates'

- Goal: Fit the Dalitz plot distributions of $D^0 \rightarrow K_S \pi \pi$ from B^- and B^+ decays to extract r_B , δ_B and γ
- Complication: The Maximum Likelihood fit overestimates r_B and underestimates the error of γ
- Solution: Write the Likelihood as a function of the cartesian coordinates x_{\pm} , y_{\pm} :

$$\begin{aligned} x_{\mp} &= r_B \cos(\delta_B \mp \gamma) \\ y_{\mp} &= r_B \sin(\delta_B \mp \gamma) \end{aligned}$$

$$\Gamma(B^+) \propto |f_+|^2 + (x_+^2 + y_+^2)|f_-|^2 + 2x_+ \operatorname{Re}(f_+ f_-^*) + 2y_+ \operatorname{Im}(f_+ f_-^*)$$

$$\Gamma(B^-) \propto |f_-|^2 + (x_-^2 + y_-^2)|f_+|^2 + 2x_- \operatorname{Re}(f_- f_+^*) + 2y_- \operatorname{Im}(f_- f_+^*)$$

$$f_{\mp} \equiv A_D(m_{\mp}^2, m_{\pm}^2)$$

Likelihood is Gaussian and unbiased in x_{\pm} , y_{\pm}

- Strategy: Extract x_{\pm} , y_{\pm} from ML fit to the $D^0 \rightarrow K_S \pi \pi$ Dalitz plot and derive r_B , δ_B and γ from x_{\pm} , y_{\pm} with stat. procedure

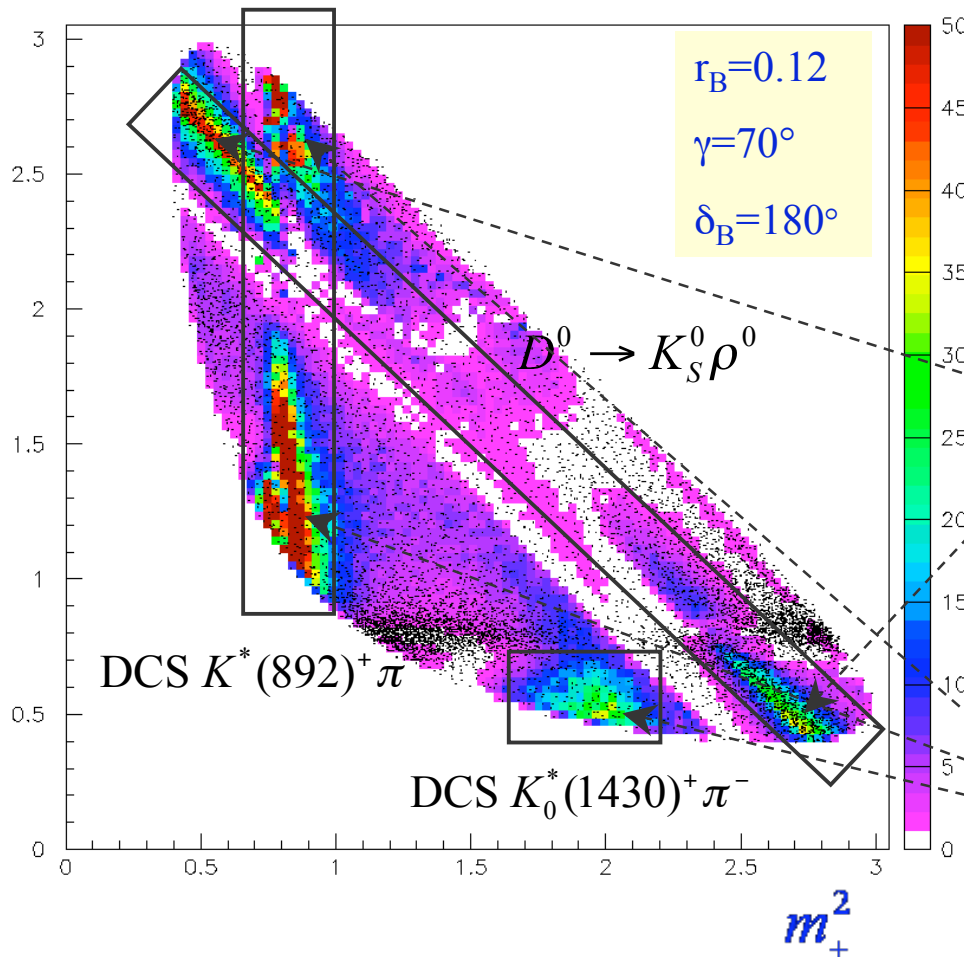
Sensitivity to γ over Dalitz plot

- Sensitivity varies strongly over Dalitz plane
- 2nd derivative of the $\log(L)$ event-by-event weighs the event

$$\sigma^2(\gamma) \sim \frac{1}{\frac{d^2 \ln(L)}{d\gamma^2}}$$

$$\text{weight} = \frac{d^2 \ln(L)}{d\gamma^2}$$

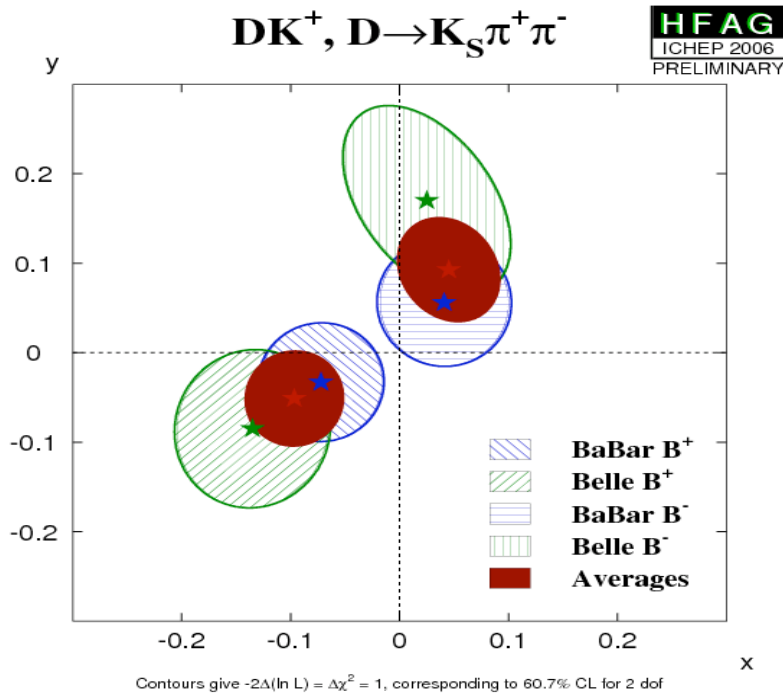
events: points (weight = 1)



Interference of $B^- \rightarrow D^0 [\rightarrow K_S^0 \rho^0] K^-$
 with $B^- \rightarrow \bar{D}^0 [\rightarrow K_S^0 \rho^0] K^-$
 \equiv GLW like

Interference of $B^- \rightarrow D^0 [\rightarrow K^{*+} \pi^-] K^-$
 (suppressed) with $B^- \rightarrow \bar{D}^0 [\rightarrow K^{*+} \pi^-] K^-$
 \equiv ADS like

γ from $B^\pm \rightarrow D_{K_S^0 \pi^- \pi^+} K^\pm$, role of r_B



BaBar: $\gamma = (92 \pm 41 \pm 10 \pm 13)^\circ$
Belle: $\gamma = (53_{-18}^{+15} \pm 3 \pm 9)^\circ$

[D*K included]

better precision of BaBar (x,y) does NOT translate to a smaller error on γ . Why?

the error of γ is \sim proportional to the uncertainty in (x,y) and inversely proportional to the distance from (0,0).

Belle measurement is consistent with larger r_B .

$\Delta x \approx \Delta y \approx r_B \Delta \theta \Rightarrow \Delta \gamma \sim 1/r_B$

Development of New Identification Selectors for K , π , P , and e

1. “*BDT Kaon*” Selectors:

- to replace *kaon neural net*, used in B-tagging
- use *Bagger Decision Tree* algorithm to separate kaon signal from pion background
- will continue to provide kaon id at 4 levels of strictness: Very Loose, Loose, Tight, Very Tight

2. “*KM*” Selectors:

- separate K , π , p , e from one another
- use multi-class learning
- will provide particle identification at 6 levels of strictness: Extra Loose, ..., Extra Tight

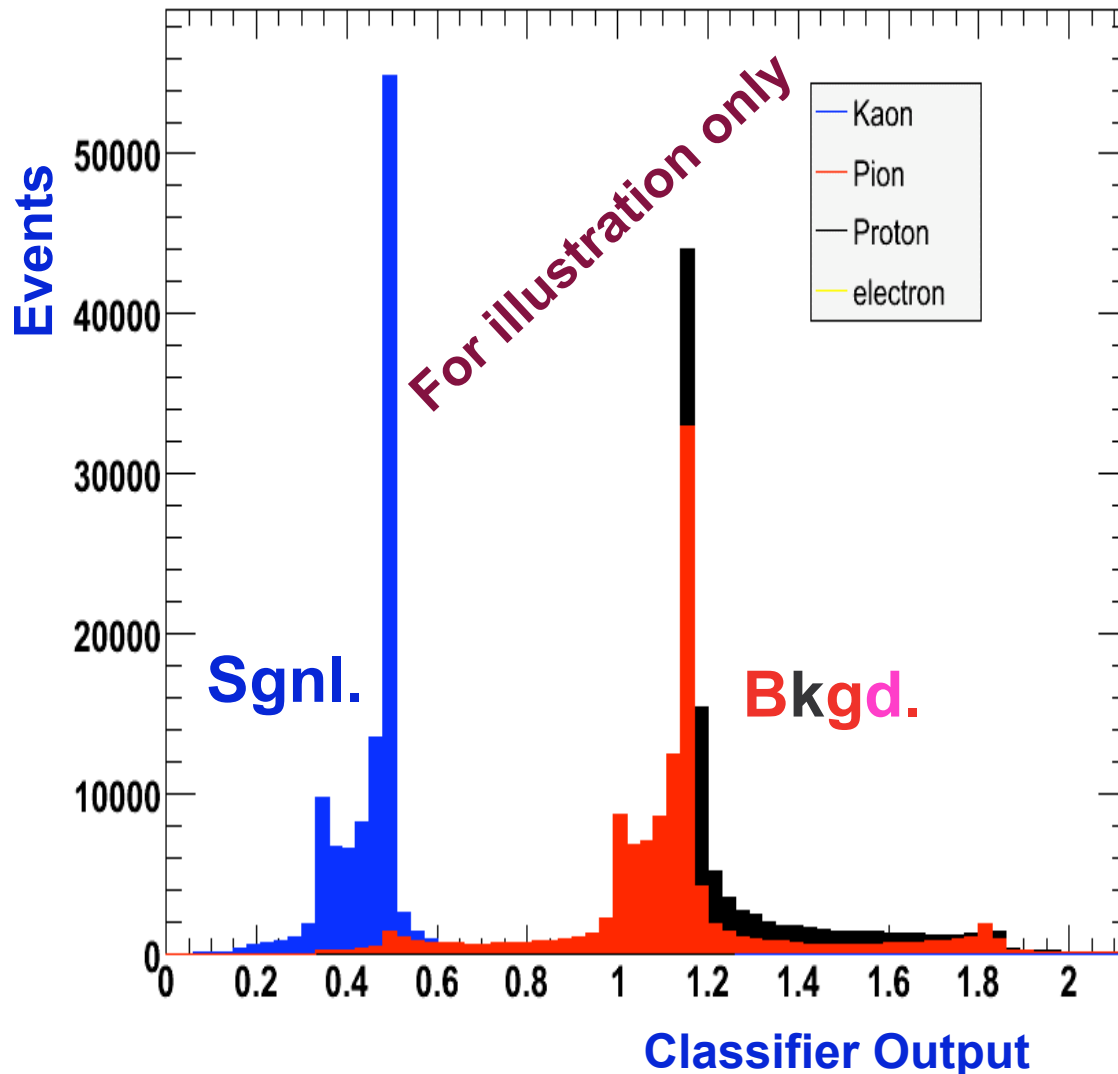
Why New Selectors ?

- **For B-tagging, need new Kaon selector to replace the old selectors.**
 - The kaon neural net hasn't been trained since circa 2001; there have been many changes in detector performance since then (e.g., **new dE/dx calibration**).
 - Trained on MC, but are used to evaluate performance in real data.
 - Give degraded performance for high-momentum tracks.
- **For kaons, protons and pions, there is only one selector of choice for analysis: Likelihood-based. There is room for improvement.**
- **For electron, the only available selector is likelihood-based.**
 - Some analyses (notably Leptonic) will benefit enormously from high-performance selectors for both low and high momentum tracks.
 - Improvement in performance needed for crucial BaBar analyses looking for New Physics, rare decays, CP violation

What is New in the New Selectors ?

- Training on “real data”.
- Include new corrections for dE/dx .
- Employ powerful statistical tools to separate signal and background, use bagging on weak classifier and multi-class training.
- For each class of particle hypothesis: “kaon”, “pion”, “proton”, and “electron”, the other three classes are treated as background for classifier training. Apart from “muon”, no additional vetoes.
- Include many additional useful input variables, including P and θ after flattening the two-dimensional $P: \theta$ distribution. No need for separate trainings in P, θ bins.

Software Implementation: StatPatternRecognition

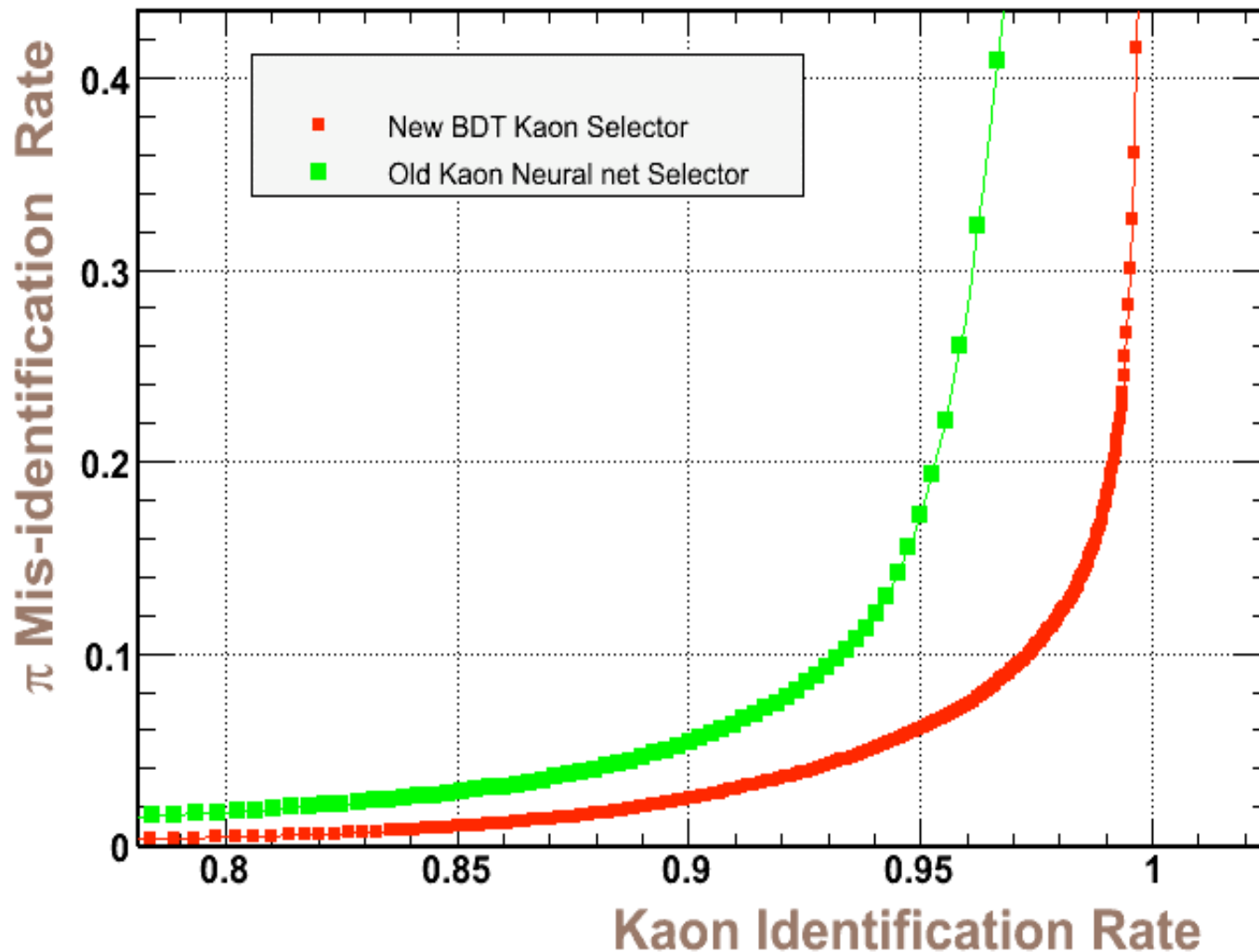


For details on the algorithms:
[arXiv:physics/0507143](https://arxiv.org/abs/physics/0507143)

(by Ilya Narsky, CalTech)

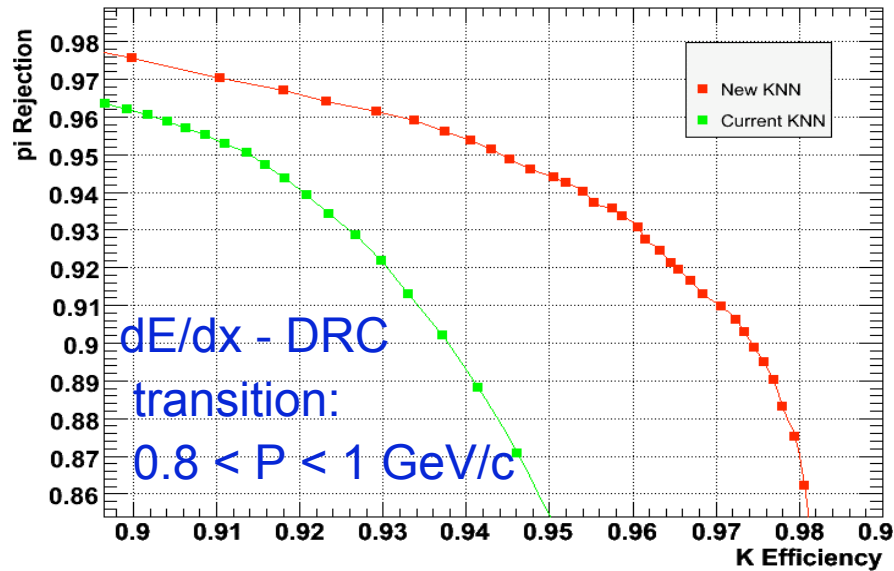
- Decision Tree splits nodes recursively until a stopping criteria is satisfied.
- Bagger decision tree divides the training data sample into a number of bootstrap replicas, and trains on each one of them separately.
- The final classification is done by majority vote.

Performance of BDT Kaon Selectors



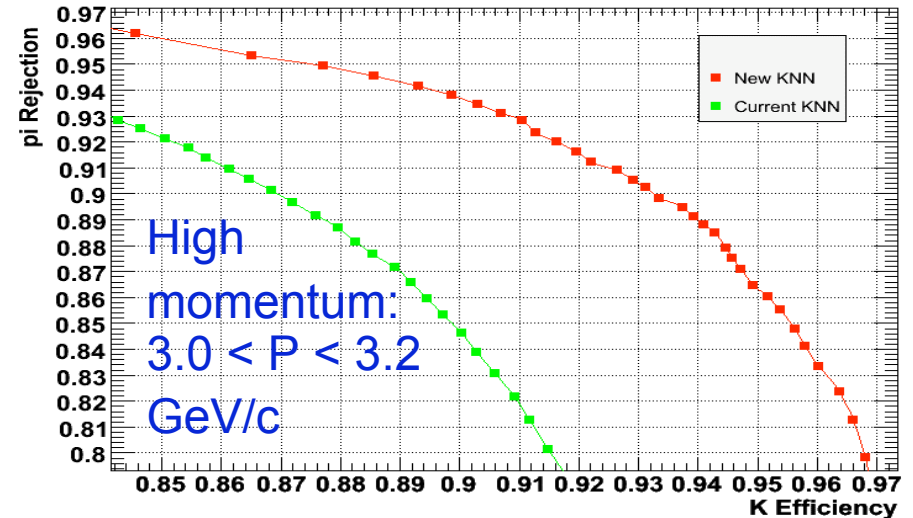
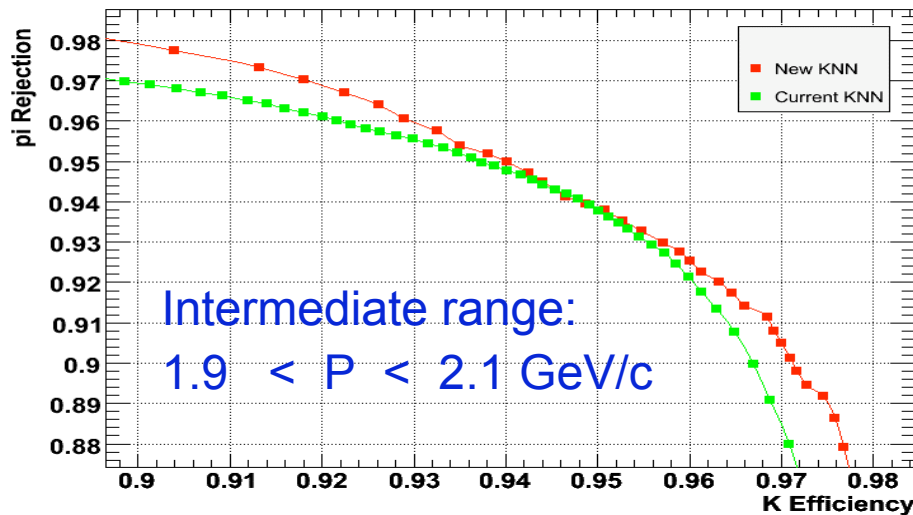
Includes all momentum and θ ranges and all tracks.

BDT Kaon Performance in Mom. Bins

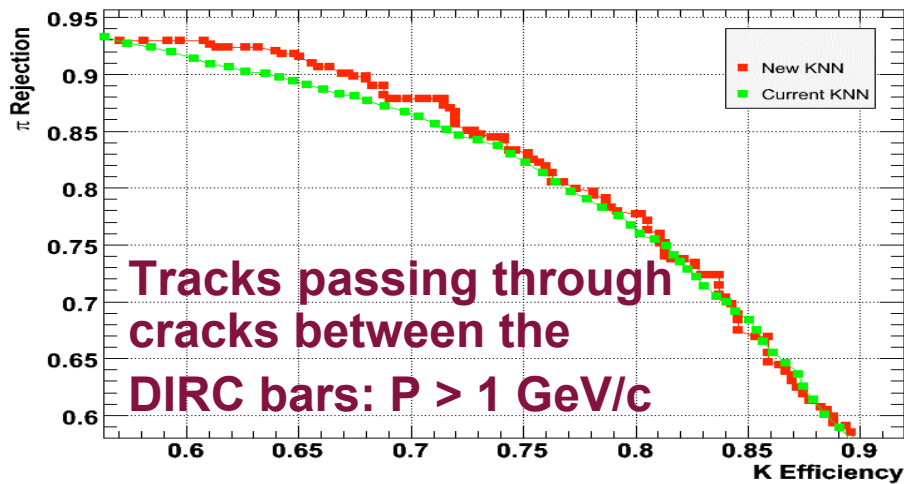
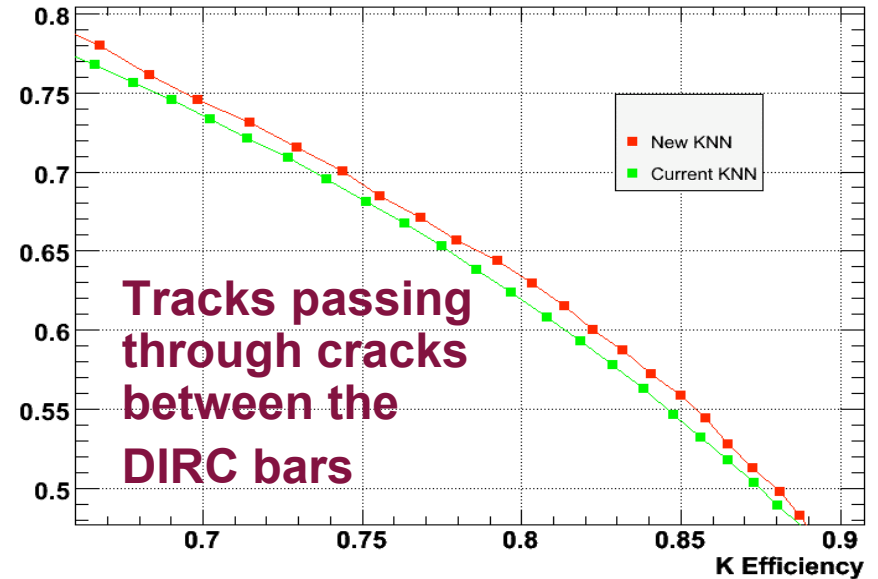
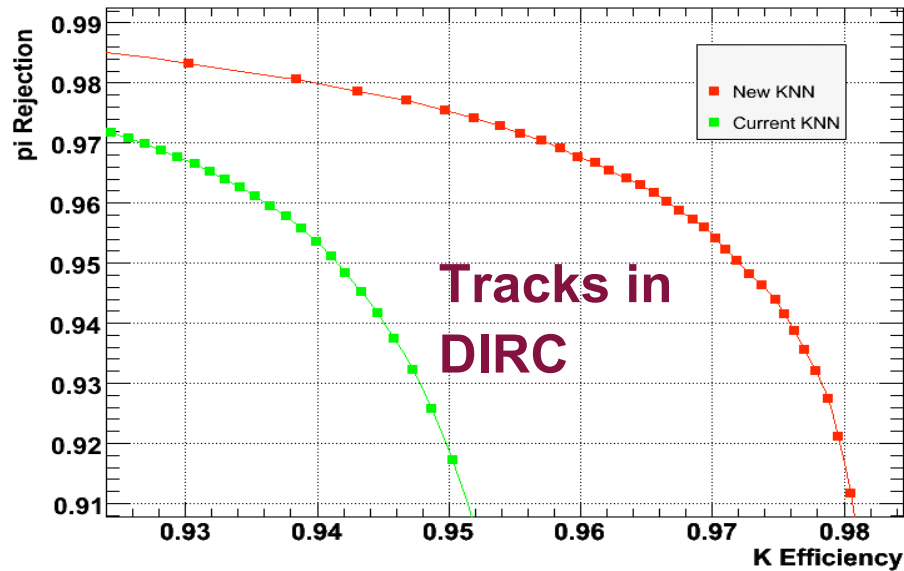


Caveat: I have changed the definition of the Y-axis variable.

The higher curve/ point represents better performance

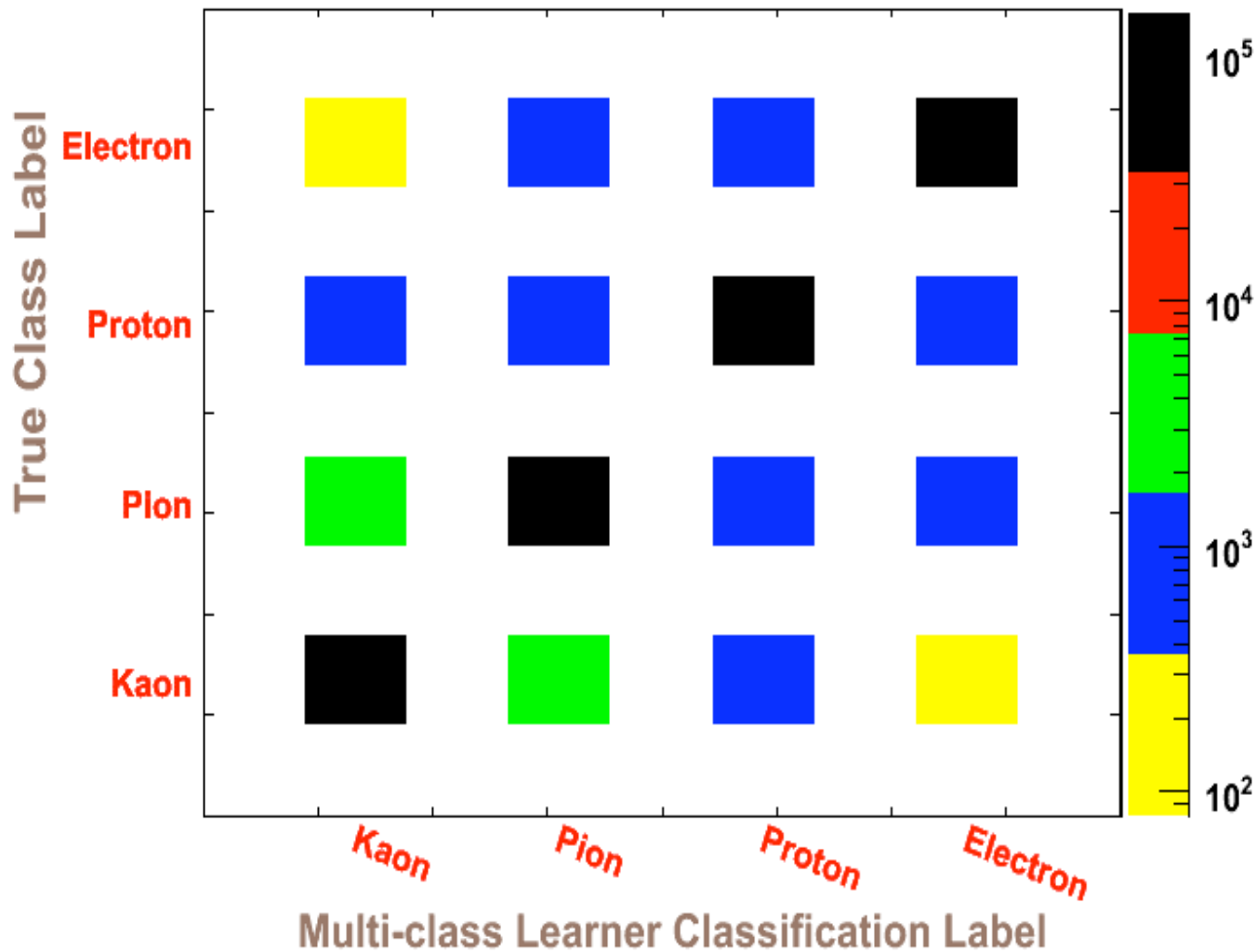


BDT Kaon Performance by Track Quality



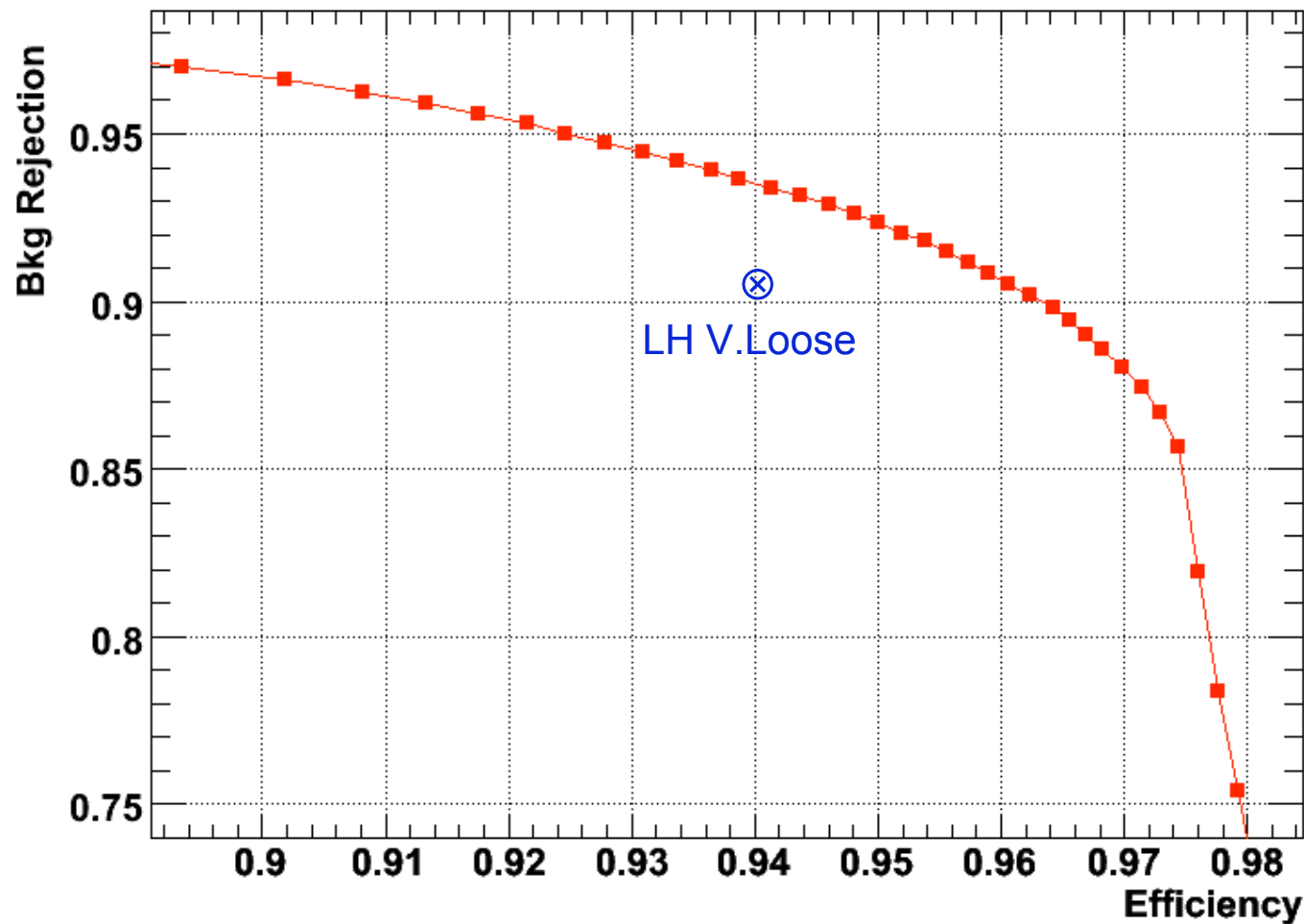
Conclusion:
Improvement in
performance
everywhere.

Performance of KM Selectors



Number of data events used for each category = 1.22×10^5

Performance of Kaon Selector

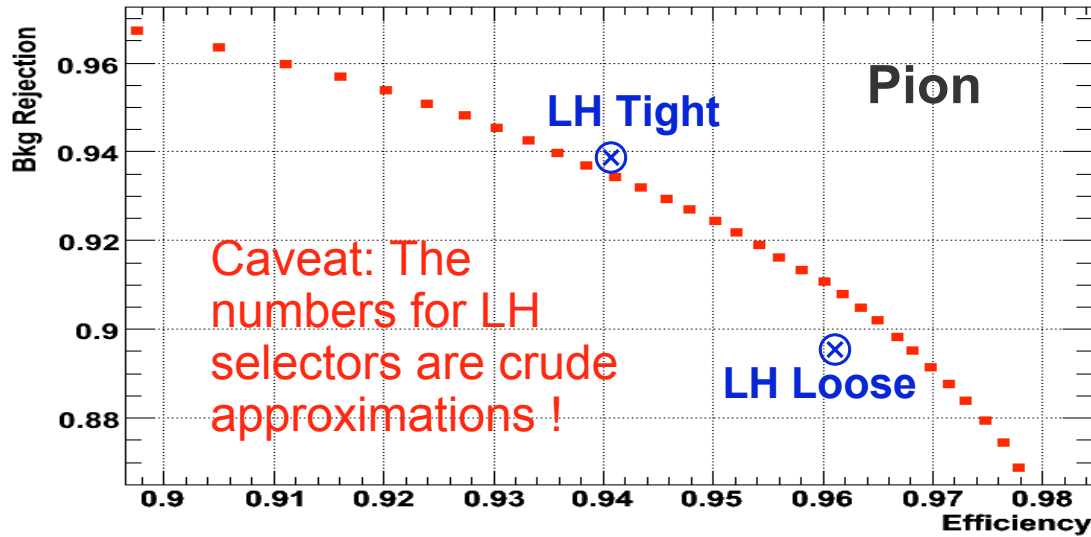


LH Loose:
Efficiency = 0.87
Pi Rej. = 0.96

LH VeryTight:
Efficiency = 0.82
Pi Rej. = 0.98

Caveat: These numbers are approximations !

Performance for Pion, Proton & Electron



Looks great ! ... But need to see performance in entire P, θ spectrum before declaring victory !

